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IMPLEMENTATION OF A PARTITIONED ALGORITHM FOR SIMULATION OF LARGE CSI PROBLEMS

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# Implementation of a Partitioned Algorithm for Simulation of Large CSI Problems

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# Summary

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This report summarizes research work on the implementation of a partitioned numerical algorithm for determining the dynamic response of coupled structure/controller/estimator finite-dimensional systems. The partitioned approach leads to a set of coupled first and second-order linear differential equations which are numerically integrated with extrapolation and implicit step methods. The present software implementation, ACSIS, utilizes parallel processing techniques at various levels to optimize performance on a shared-memory concurrent/vector processing system. The current work also generalizes the form of state estimation, whereby the Kalman filtering method is recast in a second-order differential equation equivalent to and possessing the same computational advantages of the structural equations. As part of the present implementation effort, a general procedure for the design of controller and filter gains is also implemented, which utilizes the vibration characteristics of the structure to be solved. Example problems are presented which demonstrate the versatility of the code and computational efficiency of the parallel methods is examined through runtime results for these problems. A user's guide to the ACSIS program, including descriptions of input formats for the structural finite element model data and control system definition, can be found in Appendix A. The procedures and algorithm scripts related to gain design using PRO-Matlab are included in Appendix B. In Appendix C, a stability analysis for the partitioned algorithm is presented which extends previous analysis to include observer dynamics, leading to a clearly definable stability limit. The source code for the parallel implementation of ACSIS is listed in Appendix D.

### 1.0 Introduction

The present work on the implementation of a partitioned transient analysis algorithm for the simulation of linear Control-Structure Interaction (CSI) problems has concentrated on four major areas. The initial software implementation emphasized the user-friendly aspect and a structural dynamics-oriented interface for experienced practitioners of finite element analysis programs. Another reason for a new implementation of the algorithm was that the initial architecture of the CS3 software testbed developed by Belvin and Park [1-2] had little provision for effective parallelization. CS3 also included extensive links to optimization and optimal control algorithms which were not central to the current work and proved to be a further hinderance. This new software implementation was designated ACSIS, for Accelerated Control-Structure Interaction Simulation, and led to significant improvements in speed for particular problems on conventional serial processors due to simpler and more economical storage of primary variables. ACSIS is also versatile in its usage of a general Timoshenko beam element with pin release capability and shear correction factor adjustment, and control system definition via a single data file. A preliminary Users Guide was developed for ACSIS, and the input formats were made compatible with pre/postprocessing software developed for Sun and Silicon Graphics computers so that

future versions using parallel techniques via element mesh domain decompositions can rely on the same X-Window-based I/O utilities. Table 1 documents runtime comparisions of ACSIS and CS3 on a sample 48 DOF problem simulated on a Sun 3/260 workstation using a floating point accelerator.

# 2.0 State Estimation via Second-Order Kalman Filtering

One restriction of the CS3 software testbed was the form of dynamic observer equations used in the partitioned algorithm as developed in [2]. However, Belvin and Park [3] showed that a general Kalman filtering type of state estimation was not only possible in the partitioned solution, but could be implemented at a very small additional cost in computations by a slight modification in the way the dynamical equations of the plant are cast into first-order form for filter gain design. The methods employed in [3] have been successfully implemented into ACSIS, thereby enhancing the code's ability to handle a wide variety of state estimation schemes. This is important as the application of optimal control techniques to the state estimator problem leads to this more general form, and as the restrictions of the observer used in CS3 typically meant either discarding part of the observer gain parameters, resulting in a loss in system performance.

ACSIS retains the option of using the more resricted observer form, as well as simple full state feedback (no dynamic compensation). It is clear from examining the respective equations, that for structures with stiffness-proportional damping, the only additional calculations required for the Kalman filter is the multiplication of the  $L_1$  gain matrix by the predicted state estimation error vector  $\gamma$  (see equations 25 of [3]). This is not a significant portion of the computations required at each integration step, as the dimension of  $\gamma$  is small (number of sensors). By far the major costs are for computing an internal force of the form Kq, and backsolving the factored integration matrix for the estimated displacement states. This is verified numerically in the ACSIS results of Table 1 (using a restricted form of observer) and version (A1) of Table 2. The model used in Table 1 is roughly comparable to the 54 dof truss in Table 2, and both show the additional simulation time due to state estimation is roughly the same as an additional transient analysis. Finally, the Kalman filtering equations do not lead to any additional complications in parallel implementation of the overall algorithm as compared to the more restricted second-order observer developed for CS3.

# 3.0 Parallel Implementation of ACSIS

A primary emphasis in our work dealt with the optimization of the software implementation on a concurrent processing system. The platform chosen (primarily due to availability, initially at CU and later at NASA LaRC) was the Alliant FX/8 shared memory multiprocessor system with 8 parallel processing units and vectorization capabilities. Versions of the software have been ported to the Alliant and compiled using the Concentrix FX/Fortran optimizing compiler, which has available options for automatic vectorization and concurrency of standard, problem-independent parallel computations.

The partitioned CSI algorithm has three primary levels of parallelism in its numerics which can be exploited. At the highest level is the integration of the second-order dynamical plant (structure) and filter (estimator) equations, which as designed are of roughly equivalent size. Through the algorithm, these systems are effectively decoupled and independent at each discrete time step, and thus may be handled in parallel by invoking a compiler directive in the main program, which calls the respective subroutines simultaneously and handles re-synchronization of the execution upon their return.

At a lower level of the algorithm, the structure and state estimator equations exhibit symmetric, second-order forms typical of linear structural dynamics problems. It is well known that computations related to the formation of the internal force vector, Kq, can be re-implemented at an element level [4], which, through decomposition of the element mesh [5], can be handled in parallel within exclusive subdomains. This technique becomes particularly attractive for larger problems on more massively parallel systems; in the present work, the element-by-element (EBE) technique was not as effective as other types of parallelism. It should be noted here that the partitioned algorithm employs implicit integration methods, leading to systems of algebraic equations which are factored and solved using direct, rather than iterative, numerical methods. Therefore, formulation of the internal force vector is needed only in the formation of the known (right hand side) vector for integration of the plant and filter equations. The alternative to EBE computations is multiplication of the relevant displacement vector with the global stiffness matrix stored in profile (skyline) form. To "simulate" the advantages of local memory typical in large-scale parallel processing systems, the computed element stiffnesses were saved in shared memory for the EBE calculations, thus avoiding the need to recompute this data at each integration step. In addition, a low-overhead automatic element domain decomposition was provided for the parallel EBE method.

The final and lowest level of parallelism is obviously that of the basic matrix computations such as addition, multiplication, etc. These numerical operations are inherent in nearly all areas of the software implementation, including problem preprocessing. With the very capable optimizing compiler available on the Alliant system, this parallelism was exploited through vectorization and concurrency of the nominal source code using the FX/Fortran compiler run-time options -0 -DAS -alt. The performance of the resultant executable code was examined using the Alliant's profiling capabilities, and changes to the nominal

source code, remaining compliant to F77, to maximize the identifiable concurrency and thus enhance the resultant speed. This was particularly useful in the profile matrix/vector multiply operation, whose speed is critical to the overall program performance.

# 4.0 Problem Descriptions

Three structural dynamics problems were developed for code testing at various levels of complexity. All three problems have the following common features: simulations consisted of 1000 integration steps and employed a stiffness-proportional damping. The damping was not needed for algorithm stability, but to ensure consistency between the examples and because the existence of damping in the plant equations has a strong influence on program speed. The Kalman filter models were of second-order form [2] and equivalent in size to their respective plant models. For controlled simulations, the control system began operating after 100 integration steps, and all gain matrices were full (i.e. all model states influence all actuators and are influenced by all sensors). Additional specific information for the problems follow.

# A. Axial Vibration of Elastic Bar (Spring Model)

# Nodes: 3 free, 1 fixed

# Elements: 3

# Degrees of freedom: 3

# Actuators:

# Sensors: 1

Disturbance: Initial displacement

# B. Planar Vibration of Space Truss (Truss Model)

# Nodes: 18 free

# Elements: 33

# Degrees of freedom: 54

# Actuators: 4

# Sensors: 6

Disturbance: Bang-bang type sinusoidal applied force

# C. General 3D Vibration of EPS Satellite Reboost (EPS7 Model)

# Nodes: 97 free

# Elements: 256

# Degrees of freedom: 582

# Actuators: 18

# Sensors: 18

Disturbance: Bang-bang type square wave applied force

As can be seen, the problem sizes are roughly three different orders of magnitude, with corresponding increases in the sizes of the control systems. Appendix B includes routines using Matlab for the design of control and filter gains which were used for the control system design of all three example problems. An illustration of the EPS model is shown in Figure 1.

### 5.0 Performance Assessment

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Table 2 compares CPU runtimes on the Alliant computer (using the UNIX "time" command) for distinct versions of the software. Version (A1) is the nominal F77 program code compiled without any performance-enhancing options, while version (A2) invokes automatic vectorization and concurrency of low-level, problem-independent computations such as vector addition and inner products. The performance improvements are significant, especially for the large EPS7 model, where the speed-up factor is 35-37.

Version (A3) also uses the compiler options from (A2), but in addition has a compiler directive added to the main program which allows the plant and filter integration subroutines to be called in parallel. This does not affect the transient response results as that analysis option bypasses the altered code, but for controlled response there is some effect on performance. If filtering is used, which results in a significant increase in computation, the directive can lead to some increased speed as can be seen for the spring and truss problems. There can also, however, be a reduction in performance as compared to (A2) if the finite amount of processors and vector units are used in a less efficient way. This appears to be the case for the large EPS problem, where the "overhead" introduced by the directive, and its effect on processor assignment, is greater than the improvement generated by the manually-invoked parallel construct.

Table 3 shows CPU run times for ACSIS using E-B-E computations, which, as mentioned previously did not lead to better performance on the example problems using the Alliant system. This appears to be due to the lack of effective vectorization of the individual element computations when forming the internal force via the EBE method. To determine whether the EBE method effectively lead slower speeds through increased numbers of computations, version (A2) (see above) was altered by removing compiler optimization of the profile matrix/vector multiply routine (the alternate method to EBE). The resultant runtimes matched almost exactly with those of version (A4), leading to the conclusion that both methods require roughly the same amount of computations, but differ in how they can be optimized on the Alliant system. The matrix/vector multiply operation, in this environment, can exploit both vectorization and concurrency through the complier's performance options; this can be examined in the compiler output. The EBE computations, at the element level, do not vectorize because the parts of the global displacement and force vectors being operated on per element are not contiguous. In version (A5), the elements within each subdomain of the mesh are computed in parallel, leading to some performance

Overall, versions (A2) and (A3) provide the best code performance for the hardware available. Parallelizing the observer and structure (A3) leads to mixed results; improvement for the small spring and truss problems, but not for the large EPS model. Element-by-element computations do not improve code performance over compiler optimization via vectorization and concurrency for this platform. Reimplementation of the algorithm lead to a 5:1 improvement over the CS3 testbed software on a serial computer (Table 1). Further optimization of ACSIS on the Alliant FX/8 lead to an additional 30:1 improvement in runtimes for large-order systems such as the 582 dof EPS model. Time history responses of selected variables for the example problems are shown in Figures 2 through 10. For Figures 8 through 10, the  $u_x, u_y, u_z$  displacements plotted are located at node 45, which is located at the vertex of the large antenna of the EPS model (see Figure 1).

# 6.0 Conclusions

The present work has demonstrated the efficiency of a streamlined simulation code for the analysis of large-order CSI systems and the viability of the continuous second-order Kalman filtering equations for state estimation. These methods show the versatility of the partitioned CSI integration algorithm and the promise of its application to real-time simulation. It is evident, however, that the use of element-by-element computational techniques requires the development of innovative algorithms for effective implementation on massively parallel processing systems. Future work in this area will include integrating algorithms for on-line system identification and applying these capabilities to the problem of real-time control.

# Acknowledgements

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Simulation	CS3	ACSIS
Transient	439.2	98.8
Full State Feedback	688.2	181.5
FSFB with Observer	1156.7	282.3

Table 1: Comparison of Runtime Speeds for CS3 and ACSIS on a Sun 3/260 System

	<del></del>			(1.5)
	•	(A1)	(A2)	(A3)
	Problem	Nominal	Compiler	Parallel
Model	Type	Code	Optimized	Observer
3 DOF	Transient	6.6	2.1	2.1
Spring	FSFB	8.0	3.3	3.3
	K. Filter	12.3	3.5	3.3
54 DOF	Transient	78.2	5.7	5.6
Truss	FSFB	97.1	9.4	10.2
	K.Filter	170.7	13.0	· 10.7
582 DOF	Transient	3506.	98.6	100.3
EPS7	FSFB	7040.	190.2	294.5
	K. Filter	n/a	284.2	312.5

Table 2: CPU Results for Versions of ACSIS

		(A4)	(A5)	(A6)
Model	Problem Type	E-B-E Computation	Parallel E-B-E	Parallel Obs. & EBE
3 DOF	Transient	3.8	3.3	3.3
Spring	<b>FSFB</b>	4.9	4.4	4.9
	K. Filter	6.6	5.6	5.0
54 DOF	Transient	31.7	13.0	13.0
Truss	FSFB	35.5	16.9	35.6
	K.Filter	62.6	27.3	36.2
582 DOF	Transient	391.7	153.9	n/a
EPS7	<b>FSFB</b>	485.9	245.9	n/a
	K. Filter	n/a	n/a	n/a

Table 3: CPU Results for ACSIS with EBE Computations

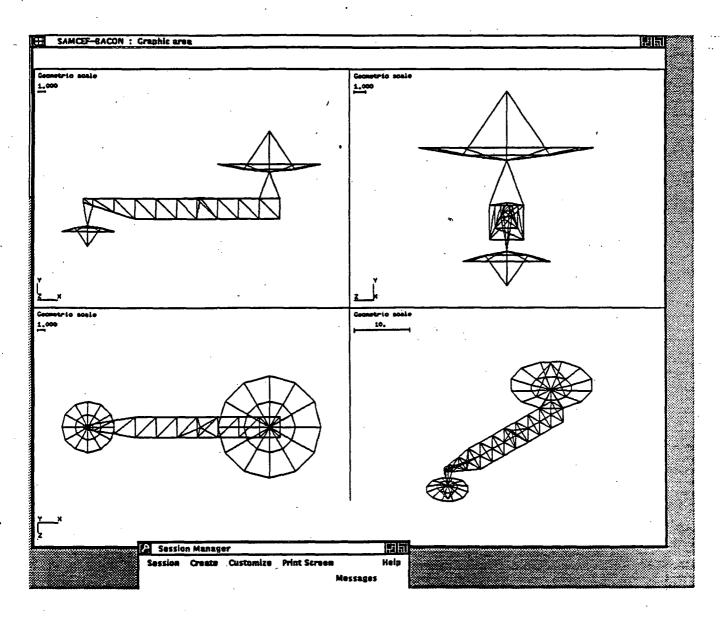


Figure 1: EPS Finite Element Model

Spring Model: Open Loop Transient Response

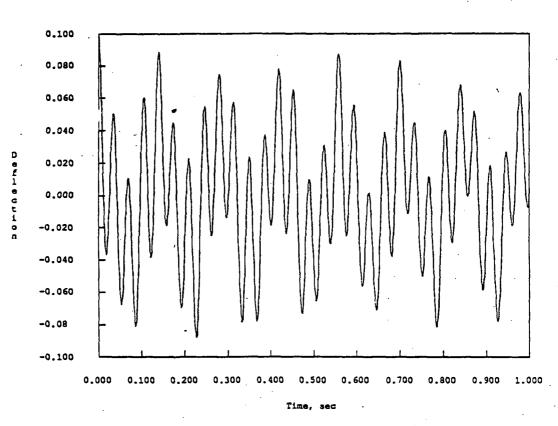
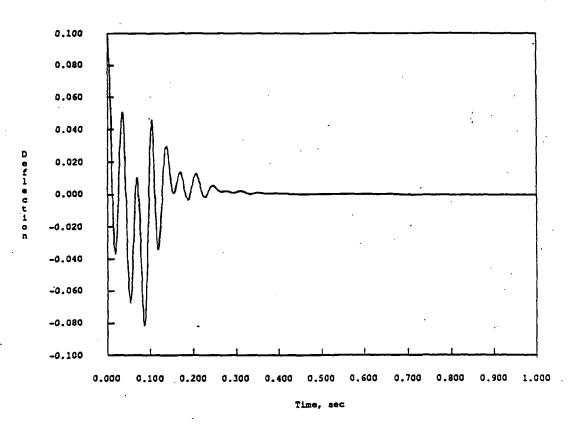


Figure 2: Spring Transient Response

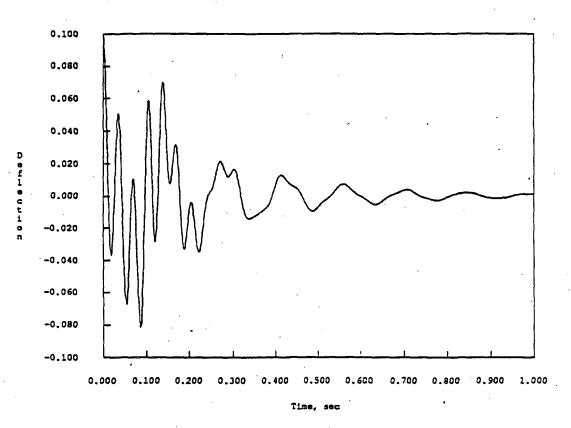
# Spring Model: Full State Feedback Response



Node 3, w

Figure 3: Spring FSFB Response

Spring Model: Controlled Response w/Kalman Filter



Node 3, w

Figure 4: Spring Response w/Filter

Truss Model: Open Loop Transient Response

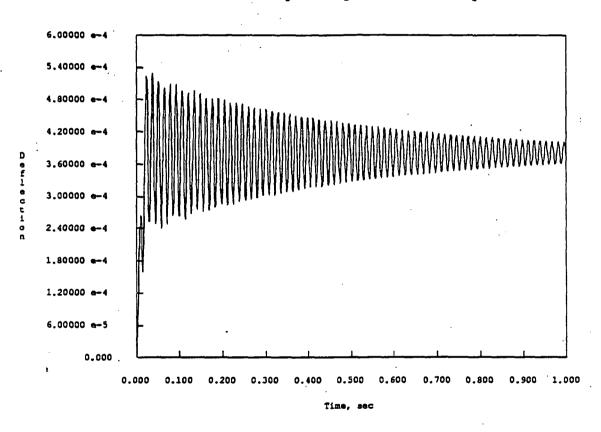
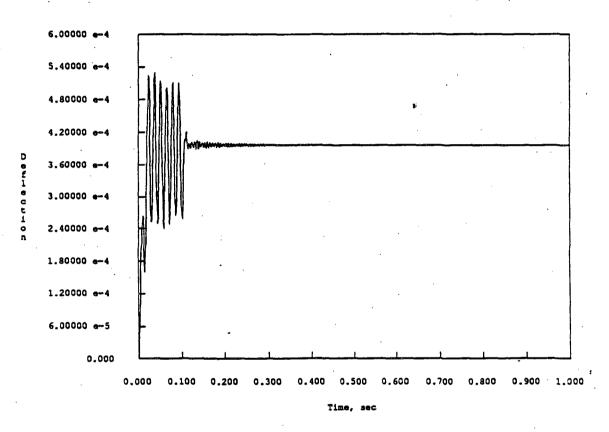


Figure 5: Truss Transient Response

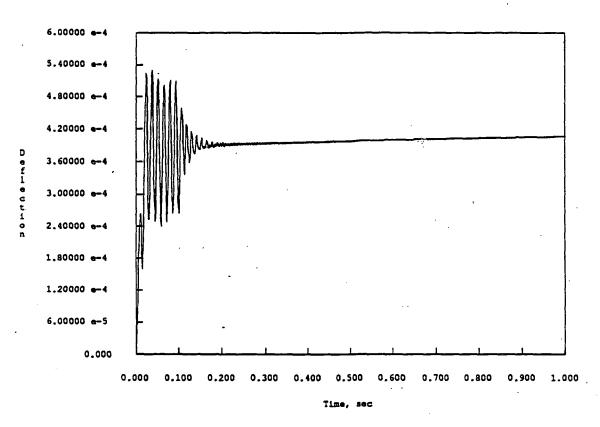
Truss Model: Full State Feedback Response



Node 9, u

Figure 6: Truss FSFB Response

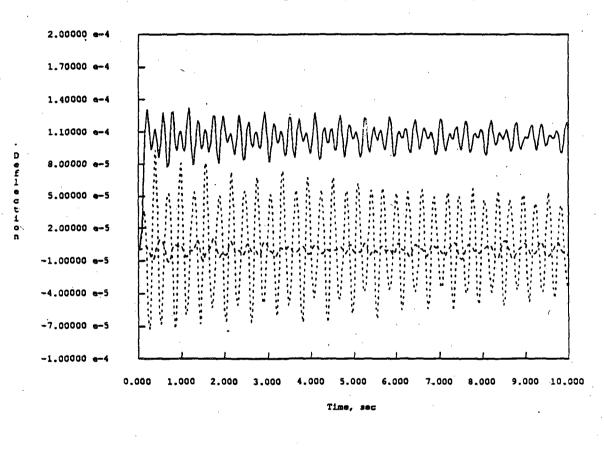
Truss Model: Controlled Response w/Kalman Filter



Node 9, u

Figure 7: Truss Response w/Filter

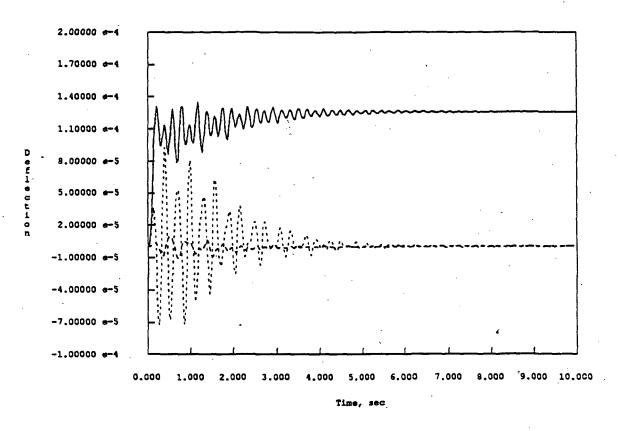
EPS7 Model: Open Loop Transient Response



Node 45, ux ---- Node 45, ux Node 45, ux

Figure 8: EPS Transient Response

EPS7 Model: Full State Feedback Response



Node 45, ux ----- Node 45, ux

Figure 9: EPS FSFB Response

EPS7 Model: Controlled Response w/Kalman Filter

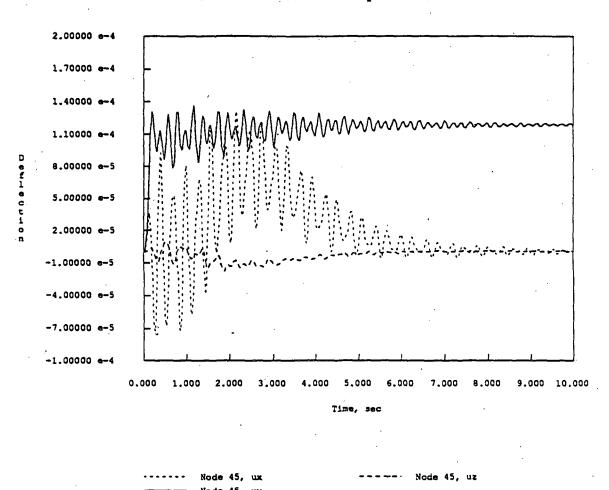


Figure 10: EPS Response w/Filter

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APPENDIX A

ACSIS User's Manual

Accelerated Control Structure Interaction Simulation

### Introduction

ACSIS is an analysis program for full-order simulation of control-structure interaction (CSI) problems. The CSI simulation is carried out using a partitioned analysis procedure which treats the structure (or plant), the observer, and the controller/observer interaction terms as separate entities. This procedure allows ACSIS to maintain relatively small, sparse matrix equations when compared to the process of assembling the computational elements into a single set of equations of motion and solving simultaneously. Although this software can also carry out modal analysis, the transient response and CSI simulation are done in real space using the entire finite element model. (For more information, see Ref. 2 of report, p. 14)

The ACSIS program is run using two previously prepared data input files and interactive input of run options. The two data input files are the finite element input file and the controller definition file.

# Interactive Options

The run options are as follows, note that no defaults exist, data must be input each time it is requested for each item requested except during a background run. Files may be given any names, example names are given only to match the truss example at the back of this manual.

# Please input analysis type:

This option is for selecting modal analysis, CSI simulation or the transient response of a structure. Not all interactive inputs are required for each analysis type.

Do you wish to save an input file? (y or n)

This option creates a file which saves all the interactive input options. ACSIS can be background run with minor option changes by editing this file and then directing the screen input to this file. This file is very different for each analysis type. (To do this run with the example names after running acsis.exe once interactively, the command would be: acsis.exe <INP\_truss> &.

Name of save input file? (filename)

This question asks for the name under which to save the interactive input. example name: INP\_truss

Finite Element Model Input File Name (filename):

This file should contain all the finite element nodes, mesh, materials, properties, lumped inertias, fixations, and initial velocity and displacement conditions. It must be prepared in advance in the card format specified later. example name: FEM\_truss

Number of modes desired? -

This only appears in the modal analysis to request the number of modes to be output. The actual analysis is carried out with double this number of modes for accuracy.

Controller Definition File Name:

This only appears for the CSI simulation. The file should contain the actuator and sensor locations, control gains, and observer gains. It also must be prepared in advance in card format. example name: CON\_truss

Please input type of control::

This option is for selecting the form of control law equations used in the CSI simulation. Full state feedback uses the current states of the plant (structure) to determine the control via constant gain matrices. Second-order observer uses only the L2 filter gain matrix of a Kalman filtering type of state estimation where the state variables are position and velocity. The Kalman filter option allows the use of a full set of filter gains, but the gain design must come from a alternate variable casting using position and generalized momenta.

Initial time, final time, control-on time, step size:

Data format is four columns for CSI, but only three columns for transient response since the control-on time part is deleted.

Forcing function ID, scale factor, damping coeff- a,b:

In order for any time dependent forcing function to be easily implemented despite variable time step sizes, the forcing functions must be entered into the subroutine forces.f. The format is to assign each new forcing function an ID number in a elseif statement. An example of forces.f is included at the back of the manual. Then forces.f must be recompiled into an object file and acsis.exe relinked. This is easily done by typing make which detects changes to the fortran files and does only the necessary compiling. A particular forcing function is chosen by entering its ID number in the first column, in addition the force can be scaled by a constant using the scaling factor in the second column. The Rayleigh damping coefficients a and b are the third and fourth columns.

# Phase lag fix? (y or n):

Specifies whether to include an extra iteration of control and sensor state prediction at each integration step to improve accuracy. Not generally needed unless the user is investigating the source of instability in a simulation and needs to test the sensitivity of the response to the partitioned algorithm's extrapolation method.

# Gain scale factors (4 total):

These scaling factors are, in order: the F1 control gain matrix (displacement), F2 control gain matrix (velocity), L1 and L2 state estimator filter gain matrix. This question appears only for CSI.

ACSIS has two types of output options. The first is the displacement or velocity motion of up to twenty separate degrees of freedom. Interactive questions are, 'Number of displacement results to output (max 10)' followed by as many 'Input node #, dof for displacement output #' as necessary. Then these repeat for velocity results. The name of the file where the output will be stored is requested by 'Output file name? (filename).' example name: OUT\_truss. The second output option saves the displacement of all nodes at any time step where output is sent (see next entry). The format is suitable for animation of the entire structure. Question asks 'Animation Output? (y or n)' then for an animation filename if necessary.

# Send output every how many steps?

This option affects both output options to reduce the size of the output and animation files. It causes output to only be sent after a integer number of time step iterations. To get output each time step, simply enter 1.

# Finite Element Input File

The finite element input file consists of title cards followed by columns of data. The title cards can be in any order, but they must be all capitalized with the appropriate number of columns of data for each card. The program reads rows of data until encountering a new card. Data which represents an integer value may be entered with a decimal point while real data may be entered without a decimal point as necessary. Any line beginning with a \* anywhere in the file is ignored and can be used to insert comments. Any blank line will result in a read error.

#### NODES

Each node must be defined on a separate line. Columns can be separated by any number of spaces or a comma. Data format is four columns: node number, x-coordinate, y-coordinate, z-coordinate.

#### TOPOLOGY

Each element must be defined on a separate line. Truss elements require two nodes then two columns of zeroes. (Truss elements would also require pin releases in ATTRIBUTES below.) Beam elements require two nodes then a third reference node representing a point in the xz plane of the beam and then a column of zeroes. Element type refers to finite element formalation. (Currently only type 1 = timeshenko beam element is now available.) Data format is six columns: element number, element type, node #1, node #2, node #3, node #4.

#### **ATTRIBUTES**

Each element is characterized by an ID number from each of the MATERIAL and PROP-ERTIES cards below. Each element also has six pin release codes. The first code is for long itudinal stiffness, the second code is for torsional stiffness, the third and fifth codes are bending stiffness at each end in the y direction and must be the same value, and the fourth and sixth codes are for bending stiffness in the z direction and also must be the same. (0 is stiff, 1 is released.) Data format is nine columns: element number, material type, property type, and six pin release codes.

#### MATERIAL

The material data is formatted in four columns: material type, Young's modulus, shear modulus and density of the material.

#### **PROPERTIES**

The properties data is formatted in six columns: property type, cross sectional area of the element,  $I_y * I_z$ ,  $I_y$ ,  $I_z$ , shear shape factor SSF2, shear shape factor SSF3.

## FIXITY

Nodes with any fixations are defined here in the finite element file. The nodes must be entered with the fixity of all six of their DOF's, restrained or not. (1 is restrained, 0 is free) Data format is seven columns: node number, x, y, z,  $\phi_z$ ,  $\phi_y$ ,  $\phi_z$ .

#### INERTIA

All lumped inertias must be entered with each separate DOF on an individual line. Therefore a single node could take up to six lines to define. Data format is three columns: node number, DOF number (1-6), and value of inertia.

#### INITIAL CONDITIONS

All initial displacement and velocity conditions are entered into the finite element file. Data format is four columns: node number, DOF number (1-6), initial displacement, and initial velocity.

#### END

End of file.

### Controller Definition Cards

The controller defintion file also consists of title cards followed by data entry. Each card must be followed by the appropriate number of columns of data and in some cases the appropriate number of rows. Integers can be entered in real format and vice versa if necessary. Any blank line will result in a read error.

#### NACT

Number of actuators in the entire control system.

#### BMAT

This entry creates the actuator position matrix or B matrix. There should be one row for each actuator, data format is four columns: node number, DOF number (1-6), actuator number, and sensitivity.

#### NSEN

Number of sensors in the entire controls system.

### HDMA

This entry creates the matrix of displacement sensor locations. One row per displacement sensor, data format is four columns: node number, DOF number (1-6), sensor number, and sensitivity.

#### HVMA

This entry creates the matrix of velocity sensor locations. One row per velocity sensor, data format is four columns: node number, DOF number (1-6), sensor number, and sensitivity.

#### F1GA

This is a list of the F1 or displacement control gains. The data format is four columns: node number, DOF number (1-6), actuator number, and value of gain.

#### F2GA

This is a list of the F2 or velocity control gains. The data format is four columns: node number, DOF number (1-6), actuator number, and value of gain.

#### L1GA

This is a list of the state estimator L1 filter gains. The data format is four columns: node number, DOF number (1-6), actuator number, and value of gain.

### L2GA

This is a list of the state estimator L2 filter gains. The data format is four columns: node number, DOF number (1-6), actuator number, and value of gain.

#### END

End of file.

# Examples

This section includes all the files and procedures needed to run all three analysis on a simple elastic bar problem. The naming of the files is a simple and easy to remember system, however no particular format is necessary.

The finite element file was created simply by typing the node locations, connectivity (topology), etc. with a text editor.

# File: FEM\_spring

# MESH NODES 0.00 0.00 0.00 1.00 0.00 0.00 2.00 0.00 0.00 3.00 0.00 0.00 TOPOLOGY 1 1 2 3 3 **ATTRIBUTES** 1 1 1 . 0 1 1 1 MATERIAL 1000. 0.0 0.0 **PROPERTIES**

The modal analysis only requires the number of modes desired in addition to the finite element file. The file INP\_spring0 documents the interactive inputs used in the modal analysis. The results are saved in file EIG\_spring.

```
File: INP_spring0
```

-1
n
 \* ACSIS input file, two lines above are
 \* analysis type and save input file. Do
 \* not change them by editing this file.
 \* Finite element input file?(filename)

FEM\_spring
 \* Number of modes desired?
3
 \* Output file?(filename)

File: EIG\_spring

EIG\_spring

# SUBSPACE ITERATION ROUTINE

NB OF EIGENVALUES= 3
NB OF VECTOR= 3
NB OF DOF= 3
TOLERANCE= 1.000E-04
NB OF RIGID MODES= 0

ITERATION NO 1

1.000E+00 1.000E+00 1.000E+00 ITERATION NO 2

1.297E-14 3.194E-14 3.899E-14

#### EIGEN ANALYSIS RESULTS:

F1 4 44 44 44 44 44 44 44 44 44 44 44 44	4754	NUMINA	······································			P			
	,			RADIAL		CYCLIC			
MODE		EIGEN	VALUE	FREQUENC	CY	FREQUENCY			
-	•			49444444444	<b>20</b> 420	***************************************			
1	,	1980.	6	44.504	•	7.0831			
. 2	?	15550	•	124.70		19.846			
3	3	32470	•	180.19		28.679			•
EIGEN	VE	CTORS:							
1		2.3305	1.8	689	-1.0372	2 .	0.	(	0.
2	<b>?</b>	1.8689	-1.0	372	2.3305	5	0.	(	0.
3	}	1.0372	-2.3	305	-1.8689	•	0.	(	0.
MASS	MA	TRIX DIA	GONAL:						
2	1	3 1.	00000000	0000D-01					
3	1	2 1.	00000000	0000D-01		•		•	•
4	1	1 1.	00000000	0000D-01					

To run the transient response of the structure, a forcing function or initial condition would be needed to excite the structure. An initial condition would be added to the finite element file. A forcing function must be added to forces.f with a new ID number, then this number given as interactive input. In this case, an initial displacement acts on the second degree of freedom, which is defined in the finite element model input file. The file INP\_spring1 documents the interactive inputs used in the transient analysis.

# File: INP\_spring1

-3 n

- \* ACSIS input file, two lines above are
- analysis type and save input file. Do
- not change them by editing this file.
- \* Finite element input file?(filename)

#### FEM\_spring

- \* Initial, final, step size?
- 0.00000000 1.00000000 0.00100000
  - \* Forcing function, scale f, damping a,b?
- 0 0.000000 0.00000000 0.00002000
  - \* Output file name?(filename)

### OUT\_spring

\* Number of displacement outputs?

1

3 1

\* Number of velocity outputs?

```
0
```

1

\* Send output every how many steps?

\* Send animation output?(y or n)

n

In addition to the finite element file, the interactive input, and an excitation, CSI simulation requires a controller definition file. A full state feedback controller for the truss structure is defined in CON\_spring.

File: CON\_spring

```
NACT
 1
BMAT
 3 1 1 1.0
F1GAIN
  2
              193,31415000000
        1
              1574.6315000000
                                            i.
             -1669.0460000000
F2GAIN
              20.774256000000
  3
              27.790403000000
              10.780212000000
NSEN
 1
TAMVH
 3 1 1 1.0
L1GAIN
              8.792890900000D-02
  2
        1 -
             -4.8807901000000D-02
              3.010273500000D-03
L2GAIN
        1
              1.038093200000D-01
  2
              6.1410130000000
             -3.0608725000000
END
```

Then if acsis.exe is run interactively and the input is saved, the file INP\_spring2 can be produced. The file could be edited to change the input files, the output file, the forcing function ID, the length of simulation, control-on time, etc. Then to run it again, type acsis.exe<INP\_spring2> scr &. The scr is a scratch file which will store the screen output.

File: INP\_spring2

```
ACSIS input file, two lines above are
           analysis type and save input file. Do
        * not change them by editing this file.
        * Finite element input file?(filename)
FEM_spring
        * Controller file name?(filename)
CON_spring
           Please input type of control:
           Initial, final, control-on, step size?
    0.00000000
                  1.00000000
                                0.10000000
                                              0.00100000
           Forcing function, scale f, damping a,b?
           0.000000 0.00000000 0.00002000
       * Phase lag fix?(y or n)
n
           Gain scale factors (4 total)?
    1.00000000
                                1.00000000
                  1.00000000
                                              1.00000000
           Output file name?(filename)
OUT_spring
           Number of displacement outputs?
   1
           Number of velocity outputs?
```

Send output every how many steps?

Send animation output?(y or n)

# APPENDIX B

Matlab Procedure and Scripts for Controller and Kalman Filter Gain Designs

### Introduction

In order to retain simplicity in the ACSIS code for parallel implementation purposes, no control system design algorithms were included. Instead, using modal data output from the eigenmode analysis module of ACSIS, a procedure was developed using the Pro-Matlab and its Control System Toolbox, which includes algorithm scripts for optimal control solutions via the solution of an algebraic Ricatti equation. In order to accommodate large order dynamical systems, the design is accomplished in the uncoupled normal modes domain, using the available lowest eigenmodes from ACSIS.

The procedure begins by copying and editing the mode data output from ACSIS (see the listing for EIG\_spring in Appendix A) into readable variables for input to Matlab. The typical approach was to create one file as a Matlab script (i.e. a ".m" file), with the eigenvalues, eigenvectors, and mass/dof data from ACSIS at the beginning, followed by actuator and sensor influence matrices (related to the physical degrees of freedom), the objective function weighting matrices, and the function which calls other Matlab scripts to determine the solution. An example of the above input for the spring problem described in Appendix A is in file EIG\_spring.m, which is listed below. Compare this the the ACSIS mode data output shown in Appendix A to see how the editing was accomplished, and the additional control design data added

# File: EIG\_spring.m

```
lam = [
          1980.6
          15550.
          32470.
                    ];
                     1.8689
v1=[1
        2.3305
                                  -1.0372
                                                    ٥.
                                                                 ٥.
        1.8689
                    -1.0372
                                   2.3305
                                                    ٥.
                                                                 0.
        1.0372
                                  -1.8689
                                                    ٥.
                                                                 ٥.
                                                                       ];
                    -2.3305
m=[ 2
                1.000000000000D-01
        1
           3
        2
             1.00000000000D-01
             1.00000000000D-01];
        1
t=[v1(:,2:4)];
qb=zeros(3,1);
qb(2,1)=1.0;
hd=zeros(1,3);
hv=zeros(1,3);
hv(1,2)=1.0;
qv=[1;.5;.1];
q=diag([qv;qv]);
r=.0001*eye(1);
[f1,f2]=mlqr(lam,t,m,qb,q,r,3);
qv=[1;1;1];
q≈diag([qv;qv]);
r=100*eye(1);
[k1,k2]=mkf(lam,t,m,hd,hv,q,r,3);
save flout f1 /ascii
save f2out f2 /ascii
```

The scripts mlqr.m and mkf.m were written to accept as input the vector of eigenvalues, the eigenvector matrix (orthogonal vectors stored in columns), a matrix of node, component, d.o.f, mass data, and the actuator (or sensor) influence matrix and weighting matrices. The scripts output the gain results in four-column arrays, with one gain per row, and the corresonding node number, displacement component, and actuator (or sensor) identification. The top-level problem script (listed above) then saves the output in external files and the analysis is complete. The design scripts (listed below) also include checks on controllability and observability of the system based on the modal data and influence matrices defined, and produce plots of the closed loop poles resulting from the gain design. This aids the analyst in assessing the expected performance (and stability) of the exact system before moving the data back to ACSIS for simulation. The script contrank m finds the rank of the controllability matrix through iterative rank calculations of submatrices so as to avoid the illconditioning experienced in the full matrix. This is both faster and more accurate for determining whether a particular actuator placement has full control of the included structural modes.

# File: mlqr.m

```
function[Flout,F2out]=mlqr(lam,t,m,qb,Q,R,nmode)
  Controller gain design for second-order
%
    structural system via given eigenmodes.
   Gains are transformed to be coefficents
%
   of structural variables (disp, velocity);
    i.e. plant is second-order, of size ndof.
  Arguments:
%
%
   lam: vector of eigenvalues (nmode x 1)
   t: matrix of eigenvctors (ndof x nmode)
ሂ
   m: mass diagonal and dof mapping info (ndof x 4)
%
   qb: actuator position influence matrix (nact x ndof)
%
    Q: optimal design state weighting matrix (2*nmode x 2*nmode)
   R: optimal design feedbk weight. matrix (nact x nact)
%
%
%
   Flout: F1 gain matrix for 2nd-order plant
   F2out: F2 gain matrix for 2nd-order plant
%
  Written by K.F. Alvin
format short e
nmodmax=length(lam);
[ndof,nact] = size(qb);
  Variables:
   mass: mass matrix
```

```
A: state transition matrix
    B: actuator influence matrix
    G: control gain matrix
massd(m(:,3))=m(:,4);
mass=diag(massd);
A=[zeros(nmode),eye(nmode);-1*diag(lam(1:nmode)),zeros(nmode)];
Amax=[zeros(nmodmax),eye(nmodmax);-1*diag(lam),zeros(nmodmax)];
B=[zeros(nmode,nact);t(:,1:nmode)*qb];
Bmax=[zeros(nmodmax,nact);t'*qb];
disp('Number of structural modes and actuators used:')
disp([nmode,nact])
disp('Rank of the controllability matrix:')
disp(contrank(A,B))
disp('Determining controller gains for given system...')
G=lqr(A,B,Q,R);
wmax=1.1*max(sqrt(lam));
axis([-wmax,wmax,-wmax,wmax]);
plot(eig(A-B+G),'+')
grid
title('Roots of controlled system')
hold
pause
   partition gain matrix
G1=G(:,1:nmode);
G2=G(:,nmode+1:nmode+nmode);
   Transform resultant gain matrices for use in
    partitioned csi algorithm using second-order
    structure(plant) equations.
disp('Mapping gains back to physical domain...')
f1=G1+t(:,1:nmode)'*mass;
f2=G2*t(:,1:nmode)'*mass;
   find modal damping ratios of controller for calulated gains:
Gmax=[f1+t,f2+t];
lambda=eig(Amax-Bmax+Gmax);
plot(lambda,'*')
pause
nfreq=sqrt(imag(lambda).^2 + real(lambda).^2);
mdamp=-real(lambda)./nfreq;
disp('Resultant modal damping ratios for controller:')
disp([' Damping ',' Damped Freq (rad/s) '])
disp([mdamp,nfreq.*sqrt(1-mdamp.^2),lambda])
bdamp=max(-2*mdamp./nfreq);
disp('Estimated minimum stiffness damping coefficient necessary')
disp(' to stabilize residual modes due to gain roundoff accumulation:')
disp(bdamp)
disp('Writing gains in node correspondence output form...')
```

```
Flout=zeros(nact*ndof,4);
F2out=zeros(nact*ndof,4);
for i=1:nact;
  kmin=(i-1)*ndof+1;
  kmax=i*ndof;
  F1out(kmin:kmax,:)=[m(:,1:2),i*ones(ndof,1),f1(i,m(:,3))'];
  F2out(kmin:kmax,:)=[m(:,1:2),i*ones(ndof,1),f2(i,m(:,3))'];
end;
disp('Finished mlqr')
```

### File: mkf.m

```
function[L1out,L2out] = mkf(lam,t,m,hd,hv,Q,R,nmode)
  Kalman filter design for second-order
    structural system via given eigenmodes
ሂ
    and transformed to independent
۲
   displacement/gen. momentum variable
    casting for partitioned csi transient
ኧ
ኧ
    analysis. See Belvin/Park paper for
    filter variable definitions.
%
%
   Arguments:
%
٧,
   lam: vector of eigenvalues (nmode x 1)
%
    t: matrix of eigenvetors (ndof x nmode)
   m: mass diagonal and dof mapping info (ndof x 4)
   hd: sensor position influence matrix (nsen x ndof)
    hv: velocity position influence matrix (nsen x ndof)
    Q: optimal design state weighting matrix (2*nmode x 2*nmode)
    R: optimal design feedbk weight. matrix (nsen x nsen)
%
%
    L1out: L1 gain matrix for 2nd-order filter
    L2out:
                L2 gain matrix for 2nd-order filter
  Written by K.F. Alvin
format short e
nmodmax=length(lam);
[nsen,ndof]=size(hd);
  Variables:
   mass: mass matrix
    A: state transition matrix
    G: noise influence matrix
    C: output influence matrix
7.
   K: filter gain matrix
massd(m(:,3))=m(:,4);
mass=diag(massd);
A=[zeros(nmode),eye(nmode);-1*diag(lam(1:nmode)),zeros(nmode)];
Amax=[zeros(nmodmax),eye(nmodmax);-1+diag(lam),zeros(nmodmax)];
```

```
G=eye(nmode+nmode);
C=[hd*t(:,1:nmode),hv*t(:,1:nmode)];
Cmax=[hd*t,hv*t];
disp('Number of structural modes and sensors used:')
disp([nmode,nsen])
disp('Rank of the observability matrix:')
disp(contrank(A',C'))
disp('Determining filter gains for given system...')
K=1qe(A,G,C,Q,R);
   partition gain matrix
K1=K(1:nmode,:);
K2=K(nmode+1:nmode+nmode.:);
Kmax=[K1;zeros(nmodmax-nmode,nsen);K2;zeros(nmodmax-nmode,nsen)];
  find modal damping ratios of filter for calulated gains:
lambda=eig(Amax-Kmax*Cmax);
plot(lambda.'+')
hold
pause
al=-real(lambda);
b1=imag(lambda);
disp('Resultant modal damping ratios for filter:')
disp([' Damping ',' Freq (rad/s) '])
disp([a1./sqrt(a1.^2+b1.^2),b1])
% Transform resultant gain matrices for use in
    partitioned csi algorithm using second-order
    Kalman filter approach.
disp('Mapping gains back to physical domain...')
li=t(:,1:nmode) *K1;
12=mass*t(:,1:nmode)*K2;
disp('Writing gains in node correspondence output form...')
Liout=zeros(nsen*ndof,4);
L2out=zeros(nsen*ndof,4);
for i=1:nsen:
 kmin=(i-1)*ndof+1;
 kmax=i*ndof:
 L1out(kmin:kmax,:)=[m(:,1:2),i*ones(ndof,1),l1(m(:,3),i)];
 L2out(kmin:kmax,:)=[m(:,1:2),i=ones(ndof,1),l2(m(:,3),i)];
disp('Finished mkf')
File: contrank.m
function maxrank=contrank(a,b)
maxrank=0;
[nstate,nact] = size(b);
i=0;
```

```
mat=b;
newrank=rank(mat);
while newrank > maxrank
   maxrank=newrank;
i=i+1;
   mat=[mat,(a^i)*b];
   newrank=rank(mat);
   if newrank=nstate
       maxrank=newrank;
   end
end
```

Unfortunately, the external files created from Matlab with the gain results are written completely in terms of real numbers, whereas the first three columns are actually to be read by ACSIS as integers (they are used as indices). A separate utility was written to convert the format of these files; the source code is listed below. On Unix systems, the user simply assigns the standard input to be the current data file created by Matlab, and gives another file name for the standard output. The code is basically just a filter to change the three columns of indices to integers. The output can then be pasted directly into the control definition file used by ACSIS.

#### File: convcont.f

```
program convcont
      parameter (NMAX=100000)
      real*8 f(NMAX).v(4)
      integer node(NMAX),dof(NMAX),act(NMAX)
      n=0
100
      read (*,*,err=200,end=200) (v(i),i=1,4)
      node(n)=int(v(1))
      dof(n) = int(v(2))
      act(n) = int(v(3))
      f(n)
             =v(4)
      goto 100
200
      do 300 i=1,n
        print *, node(i),dof(i),act(i),f(i)`
300
        continue
      end
```

## APPENDIX C

Stability Analysis of a CSI Partitioned Simulation Algorithm with State Estimator The equation of the open-loop plant without passive damping in modal second-order form is

$$\ddot{q} + \omega^2 q = u \tag{1}$$

The controller uses a second-order observer to estimate the plant state, along with a full-state feedback control gain design.

$$u = -(\eta \omega^2 p + \zeta \omega \dot{p})$$

$$\ddot{p} + \omega^2 p = u + \xi \gamma$$

$$\gamma = z - \dot{p}$$

$$z = \dot{q}$$
(2)

where q and p are the plant and estimator states, respectively, u is the control force,  $\gamma$  is the state estimation error, z is the sensor output, and  $\eta, \zeta, \xi$  are gain coefficients for position and velocity feedback, and the estimator filter.

The partitioned analysis procedure uses a stabilized form of the control law and estimation error determination to reduce inaccuracies associated with the extrapolation of variables in the controller force prediction. A first-order filtering is achieved by taking the time derivative of (2a,c),

$$\dot{u} = -\eta \omega^2 \dot{p} - \zeta \omega \ddot{p}$$

$$\dot{\gamma} = \dot{z} - \ddot{p}$$
(3)

and then embedding the equations of motion through substitution for  $\ddot{p}$ . This leads to the following two coupled, first-order differential equations for the prediction of the control force u and state error  $\gamma$ .

Time discretization of (4) using an implicit midpoint rule leads to the following coupled difference equation:

$$\begin{bmatrix} 1 + \delta \zeta \omega & \delta \zeta \xi \omega \\ \delta & 1 + \delta \xi \end{bmatrix} \begin{Bmatrix} u^{n + \frac{1}{2}} \\ \gamma^{n + \frac{1}{2}} \end{Bmatrix} = \begin{Bmatrix} 0 \\ z_p^{n + \frac{1}{2}} \end{Bmatrix} + \begin{Bmatrix} \delta \zeta \omega^3 - \eta \omega^2 \\ \delta \omega^2 \end{Bmatrix} p_p^{n + \frac{1}{2}} - \begin{Bmatrix} \zeta \omega \\ 1 \end{Bmatrix} \dot{p}^n \quad (5)$$

where  $\delta \equiv \text{half-step size} = \frac{h}{2}$ . Solving this equation requires knowledge of the plant (to obtain sensor output) and observer states. These values are extrapolated as:

$$p_p^{n+\frac{1}{2}} = p^n + \delta \dot{p}^n$$

$$z_p^{n+\frac{1}{2}} = \dot{q}_p^{n+\frac{1}{2}} = \dot{q}^n$$
(6)

Using these equations to obtain  $u^{n+\frac{1}{2}}$  and  $\gamma^{n+\frac{1}{2}}$  allows the plant and observer equations to be solved independently. Midpoint time integration of (1) and (2b) leads to the following equations:

$$(1 + \delta^{2}\omega^{2}) q^{n + \frac{1}{2}} = \delta^{2}u^{n + \frac{1}{2}} + q^{n} + \delta\dot{q}^{n}$$

$$(1 + \delta^{2}\omega^{2}) p^{n + \frac{1}{2}} = \delta^{2}u^{n + \frac{1}{2}} + p^{n} + \delta\dot{p}^{n} + \delta^{2}\xi\gamma^{n + \frac{1}{2}}$$

$$\dot{q}^{n + \frac{1}{2}} = \frac{1}{\delta} \left( q^{n + \frac{1}{2}} - q^{n} \right)$$

$$\dot{p}^{n + \frac{1}{2}} = \frac{1}{\delta} \left( p^{n + \frac{1}{2}} - p^{n} \right)$$

$$q^{n + 1} = 2q^{n + \frac{1}{2}} - q^{n}$$

$$p^{n + 1} = 2q^{n + \frac{1}{2}} - q^{n}$$

$$\dot{q}^{n + 1} = 2\dot{q}^{n + \frac{1}{2}} - \dot{q}^{n}$$

$$\dot{p}^{n + 1} = 2\dot{q}^{n + \frac{1}{2}} - \dot{q}^{n}$$

Computational stability of the modal form of the CSI partitioned equations of motion using the aforementioned time discretization can be assessed by seeking a nontrivial solution of

such that

$$|\lambda| \le 1 \tag{9}$$

for stability. Subtituting (8) into (5-7), we obtain

$$\mathbf{J}\mathbf{x} = \mathbf{0} \tag{10}$$

where

$$\mathbf{x}_{1} = \begin{bmatrix} p_{p}^{n+\frac{1}{2}} & u^{n+\frac{1}{2}} & p^{n+\frac{1}{2}} & \dot{p}^{n+\frac{1}{2}} & p^{n} & \dot{p}^{n} \end{bmatrix}^{T}$$

$$\mathbf{x}_{2} = \begin{bmatrix} z_{p}^{n+\frac{1}{2}} & \gamma^{n+\frac{1}{2}} & q^{n+\frac{1}{2}} & \dot{q}^{n+\frac{1}{2}} & q^{n} & \dot{q}^{n} \end{bmatrix}^{T}$$

$$\mathbf{J} = \begin{bmatrix} \mathbf{J}_{11} & \mathbf{J}_{12} \\ \mathbf{J}_{21} & \mathbf{J}_{22} \end{bmatrix}$$
(11)

$$\mathbf{J}_{11} = \begin{bmatrix} 1 & 0 & 0 & 0 & -1 & -\delta \\ (\eta\omega^2 - \delta\zeta\omega^3) & (1 + \delta\zeta\omega) & 0 & 0 & 0 & \zeta\omega \\ 0 & -\delta^2 & (1 + \delta^2\omega^2) & 0 - 1 & -\delta \\ 0 & 0 & -\frac{1}{\delta} & 1 & \frac{1}{\delta} & 0 \\ 0 & 0 & -2 & \lambda + 1 & 0 \\ 0 & 0 & 0 & -2 & 0 & \lambda + 1 \end{bmatrix}$$
(12)

$$\mathbf{J_{22}} = \begin{bmatrix} 1 & 0 & 0 & 0 & 0 & -1 \\ -1 & (1+\delta\xi) & 0 & 0 & 0 & 0 \\ 0 & 0 & (1+\delta^2\omega^2) & 0 & -1 & -\delta \\ 0 & 0 & -\frac{1}{\delta} & 1 & \frac{1}{\delta} & 0 \\ 0 & 0 & -2 & 0 & \lambda+1 & 0 \\ 0 & 0 & 0 & -2 & 0 & \lambda+1 \end{bmatrix}$$
 (15)

A nontrivial solution to (10) is found from

$$\det \mathbf{J} = 0 \tag{16}$$

which leads to the characteristic equation

$$((1 - \delta\xi) (1 + \delta^{3}\zeta\omega^{3} - \delta^{2}\eta\omega^{2}) + \delta\xi (1 + \delta^{2}\omega^{2}))z^{4}$$

$$+ (\delta\zeta\omega (1 - \delta\xi) + \delta\xi (1 + \delta^{3}\zeta\omega^{3} - \delta^{2}\eta\omega^{2}))z^{3}$$

$$((1 - \delta\xi) (\delta^{2}\omega^{2} + \delta^{2}\eta\omega^{2}) + \delta^{2}\omega^{2} (1 + \delta^{3}\zeta\omega^{3} - \delta^{2}\eta\omega^{2})$$

$$+ \delta\xi (\delta\zeta\omega + \delta^{2}\omega^{2} + \delta^{4}\omega^{4}))z^{2}$$

$$(\delta^{2}\omega^{2} (\delta\zeta\omega) + \delta\xi (\delta^{2}\omega^{2} + \delta^{2}\eta\omega^{2}))z$$

$$+ \delta^{2}\omega^{2} (\delta^{2}\omega^{2} + \delta^{2}\eta\omega^{2}) = 0$$

$$(17)$$

where

$$\lambda = \frac{1+z}{1-z}, \quad |\lambda| \le 1 \quad \Longleftrightarrow \quad Re(z) \le 0 \tag{18}$$

Thus, a test of the polynomial equation for possible positive real roots by the Routh-Hurwitz criterion indicates that the partitioned approach as applied to the modal equations give a computationally stable solution for no velocity feedback  $\zeta=0$  provided

$$h \le \frac{2}{\sqrt{\eta}\omega} \tag{19}$$

$$h \le \frac{2}{\xi} \tag{20}$$

# APPENDIX D

ACSIS Source Code

```
File: Makefile
```

```
.SUFFIXES: .f .o

FFLAGS =

.f.o:
    fortran -c $(FFLAGS) $*.f

OBJS = acsis.o acsisout.o beam3d.o forces.o
```

addstf.o forces.o imput.o profile.o DEVENUE. prepfem.o nophlag.o read.o solver.o prepcon.o zerovect.o lu.o measure.o control.o secorder.o animout.o eigens.o singeig.o stiffrc.o estifvm.o renum.o kfilter.o

acsis.exe: \$(OBJS)

fortran -o acsis.exe \$(FFLAGS) \$(OBJS)

### File: shared.inc

```
C
C
C
C.
      shared.inc (ACSIS database)
C
C
C
C
C
    Argument definitions:
C.
                 Rayleigh damping coefficient alpha
C
                 actuator location matrix (packed storage)
C
        brow: row number of corresponding real value in b
C
                 column number of corresonding real value in b
        bcol:
C
                 number of nonzero values in b
        bval:
C
               Rayleigh damping coefficient beta
        bdamp:
        confile: controller input file name contype: id for type of control
C
C
        coxyz: array of the x,y, and z components of each node
C
        delta: one-half time step
C
C.
      delsq: one-half time step squared
C
        ec:
                  control prediction integration coefficient matrix
C
        emat:
                 array of element material types
C
                  observer construct matrix S in vector form
        eo:
C.
                 array of element property types
        eprop:
C
                  structure: construct matrix S (M+delta*D+delsq*K)
        95:
C
        etype:
                 array of element types
C.
                  array of element numbers for domain decomposition
        elnum:
C
        f:
                 vector of applied forces
        f1:
                  control gain matrix
```

```
femfile: finite element input file name
C
C
        forceid: identification number of forcing function
C
                  state correction force
        gamma:
C
        gc:
                  RHS vector for control prediction module
C
        gk:
                  RHS vector for Kalman filter momentum eqn
C
                  RHS vector for observer module
        go:
C
        gs:
                  RHS vector for structure module
C
        h:
                  time step size
C
        hd:
                  displacement sensor location matrix (packed storage)
C
        hdrow:
                  row number of corresponding real value in hd
C
        hdcol:
                  column number of corresonding real value in hd
C
        hdval:
                  number of nonzero values in hd
C
        hv:
                  velocity sensor location matrix (packed storage)
C
        FALOR:
                  row number of corresponding real value in hv
C
        hvcol:
                  column number of corresonding real value in hv
C
        hvval:
                  number of nonzero values in hv
C
        id:
                  DOF mapping array: id(comp,node $)=Global DOF $
C
        ix:
                  array of element connectivity and orientation
C
        inertia:
                  array of concentrated inertias or lumped masses
C
        jdiag:
                  array of diagonal element addresses
C
        11:
                  State estimator filter gain matrix
C
                  State estimator filter gain matrix
        12:
C
        mask:
C
        mass:
                  mass matrix M in reduced vector form
C
        mat:
                  array of different materials
C
        mlen:
                  length of global matrices in profile vector storage
C
        nact:
                  actual number of actuators
C
        ncsi:
                  actual number of actuators and sensors
C
        ndisout:
                  number of displacement results to output
C
        ndof:
                  actual number of degrees of freedom
C
        ndomain:
                  actual number of element domains (for dom. decomp.)
C
        nel:
                  actual number of elements
C
                  array of number of elements in each domain
        neld:
C
                  actual number of nodes
        nnp:
C
        DSen:
                  actual number of sensors
C
                  number of velocity results to output
        nvelont:
C
                  logical flag to signal corrector loop in measurement
        nolag:
C
        outfile:
                  output file name
C
        outlabel: array of output data requested
C
                  array of element pin release codes
C
                  Column pivoting info from FACTA
        pivot:
C
        prop:
                  array of different properties
C
        q:
                  generalized displacement vector
C
        q0:
                  initial displacement condition
C
                  gain scale factor for fi
        qalpha:
C
                  gain scale factor for li
        qalphao:
C
                  gain scale factor for 12
        qbeta:
C
        qbetao:
                  gain scale factor for 12
C
        qdot:
                  velocity vector
C
        qdot0:
                  initial velocity condition
C
        qe:
                  state estimator displacement vector
C
        qedot:
                  state estimator velocity vector
C
                  Solution vector of control module {u,gamma}
C
        scalef:
                  Scaling factor for forcing function
C
        stiff:
                  stiffness matrix K in reduced vector form
C
        tO:
                  initial time
C
        tc
                  control-on time
        tf:
                  final time
```

control gain matrix

C

12:

```
u:
             vector of control forces
Parameter definitions
  HAXACT:
            max. # of actuators
  MAICSI:
            max. combined $ of actuators and sensors
           max. # of materials and properties
  MAXDAT:
  MAXDOF:
            max. 3 of degrees of freedom
  MAXDOM:
            max. # of decomposition domains
  MAXELE:
            max. # of elements
  MAXMLEN: max. length of global vectors in reduced form
  MAXNODE: max. # of nodes
parameter(MAXDOF=3000, MAXACT=50, MAXCSI=100)
parameter(MAXNODE=1000, MAXELE=3000, MAXDAT=100)
parameter(MAIMLEN=200000, MAIDON=50, MAIMZV=200)
real *8 t0, tf, tc, h, delta, delsq, qalpha, qbeta, qalphao, qbetao
real *8 q(MAXDOF),qdot(MAXDOF),qe(MAXDOF),qedot(MAXDOF)
real *8 u(MAXACT), gamma(MAXACT), f(MAXDOF), r(MAXCSI)
real*8 es(MAXMLEN), eo(MAXMLEN), ec(MAXCSI, MAXCSI)
real=8 gs(MAXDOF),go(MAXDOF),gc(MAXCSI),scalef,pe(MAXDOF)
real * 8 mass (MAXMLEN), stif (MAXMLEN), adamp, bdamp, gk (MAXDOF)
real*8 coxyz(3, MAXNODE), mat(6, MAXDAT), prop(10, MAXDAT)
real *8 q0(6, MAXNODE), qdot0(6, MAXNODE), inertia(6, MAXNODE)
real*8 b(MAXNZV),hd(MAXNZV),hv(MAXNZV),estifm(78,500)
real *8 f1(MAXACT, MAXDOF), f2(MAXACT, MAXDOF)
real *8 l1(MAXDOF, MAXACT), 12(MAXDOF, MAXACT)
integer etype(MAXELE), ix(4, MAXELE), emat(MAXELE), forceid
integer eprop(MAXELE),pin(6,MAXELE),id(6,MAXNODE)
integer mask(MAXMODE),contype,brow(MAXMZV),bcol(MAXMZV)
integer hdrow(MAXNZV),hdcol(MAXNZV),hvrow(MAXNZV)
integer hvcol(MAXNZV), bval, hdval, hvval
integer ndof,nact,nsen,ncsi,mlen,jdiag(MAXDOF),nnp,nel,neig
integer neld(MAXDOM), elnum(MAXELE, MAXDOM), eldom(MAXELE), ndomain
integer outlabel(40),ndisout,nvelout,pivot(MAXCSI)
integer iadjcy(MAXMLEN),icount(MAXNODE+1),perm(MAXNODE)
integer xls(MAXNODE)
logical animate.nolag
character * 32 femfile, confile, outfile, animfile
COMMON /FILES/ femfile, confile, outfile, outlabel, ndisout,
               nvelout, animfile, animate, nolag
COMMON /TIMERS/ t0,tf,tc,h,delta,delsq
COMMON /STATES/ q,qdot,qe,qedot,u,gamma,f,r,pe
COMMON /FEMDAT/ mass, stif, adamp, bdamp, coxyz, mat, prop, q0, qdot0,
                 inertia, scalef
COMMON /INTEGR/ es,eo,ec,gs,go,gc,gk,pivot
COMMON /DIMENS/ ndof,nact,nsen,ncsi,mlen,jdiag,nnp,nel,neig
COMMON /CONDAT/ b,hd,hv,f1,f2,11,12,
                 qalpha,qbeta,qalphao,qbetao
COMMON /ELEDOM/ estifm, ndomain, neld, elnum, eldom
COMMON /INTGER/ forceid, etype, ix, emat, eprop, pin, id, mask,
                 contype, brow, bcol, hdrow, hdcol, hvrow, hvcol,
                 bval,hdval,hvval
COMMON /RESEQN/ iadjcy,icount,perm,xls
```

C

C

C

C

C

C

C

C

```
C=Program ACSIS
C=Purpose Accelerated CSI Simulation
C=Author K. Alvin
C=Date May 1990
C=Block Fortran
C
                                                                             C
C
      program ACSIS
                                                                             C
Ç.
                                                                             C
C
                                                                             C
C
                 2nd Order Accelerated CSI Simulation
C
C
                                                                             C
      program ACSIS
C
      GET SHARED DATA FILE
      include 'shared.inc'
      LOCAL VARIABLES
      real*8 t,z(MAXACT)
      integer n,m,runtype,outskip
C
      LOGIC
      call IMPUT(runtype,outskip)
      if (runtype) 100,200,300
C
      EIGENHODE ANALYSIS
100
      continue
      call PREPFEM
      call EIGENS
      goto 999
      CSI SIMULATION
200
      call PREPFEM
      call PREPCON
      n = 0
      m = 0
      print *,'Finished Preprocessing . . . starting simulation'
      print *,'Time =',t0
      CALL ACSISOUT(t0)
      do 250 t=t0,tf,h
        call FORCES(t+h/2)
C
      Predict CSI coupling variables u and gamma
```

```
if (t .ge. tc) then
          call MEASURE(z)
          call CONTROL(z)
          if (nolag) then
            call WOPHLAG(z)
            call CONTROL(z)
            endif
          endif
C
      Structure and observer set up for parallel execution
CVD$ CNCALL
        do 275 i=1,2
C
      Integrate Observer Equations
          if ((i .eq. 1).and.(t .ge. tc)) then
            if (contype .eq. 0) then
               call SECORDER(mass, stif, adamp, bdamp, f, go, eo, qe, qedot,
                           delta, delsq, jdiag, ndof, MAXDOF)
            elseif (contype .eq. 1) then
               call KFILTER
               endif
     Integrate Structure Equations
          elseif (i .eq. 2) then
            call SECORDER(mass, stif, adamp, bdamp, f, gs, es, q, qdot,
                           delta, delsq, jdiag, ndof, MAXDOF)
            endif
275
          continue
      PRINT TIME EACH 100 iterations
        n = n + 1 '
        m = m + 1
        if (n .ge. 100) then
          print *, 'Time = ',t+h
          n. = 0
          endif
        if (m .ge. outskip) then
          call ACSISOUT(t+h)
          write(24,'(40f12.8)') t,(z(i),i=1,nsen)
          m = 0
        endif
250
        continue
      goto 999
      TRANSIENT RESPONSE
      call PREPFEM
300
      0 = a
      print *, 'Finished Preprocessing . . . starting simulation'
      print *,'Time = ',t0
```

```
call ACSISOUT(t0)
      do 350 t=t0,t1,h
        call FORCES(t+h/2)
        call ZEROVECT(gs,ndof)
        call SECORDER(mass, stif, adamp, bdamp, f, gs, es, q, qdot,
                          delta, delsq, jdiag, ndof, MAXDOF)
C
      PRINT TIME EACH 100 iterations
        n = n + 1
        m = m + 1
        if (n .ge. 100) then
          print *,'Time * ',t+h
          n = 0
        endif
        if (m .ge. outskip) then
           call ACSISOUT(t+h)
           m = 0
           endif
350
      continue
999
      stop
      end
File: acsisout.f
C=Module ACSISOUT
C=Purpose Write desired output from ACSIS for plotting, etc.
C=Author K. Alvin
C=Date May 1990
C=Block Fortran
C
      Subroutine ACSISOUT
C
C
    . Purpose:
C
         This subroutine outputs formatted displacement and velocity
C
         results at a given time for plotting time histories. The
C
         desired output variables are defined in outlabel().
C
C
C
C
       Arguments
C
         t - time
C
      subroutine ACSISOUT(t)
      include 'shared.inc'
      real *8 t
```

```
integer i
C
      LOGIC
      write(13,'(40f12.8)') t,(q(id(outlabel(i+10),outlabel(i))),
     . is1,ndisout),(qdot(id(outlabel(i+30),outlabel(i+20))),
     . i=1,nvelout)
      write(23,'(40112.8)') t,(qe(id(outlabel(i+10),outlabel(i))),
     . isi,ndisout),(qedot(id(outlabel(i+30),outlabel(i+20))),
     . i=1,nvelout)
      write(25,'(40f12.8)') t,(u(i),i=1,nact),(gamma(i),i=1,nsen)
      if (animate) call ANIMOUT(q,id,nnp,t,15)
      return
      end
File: addstf.f
C=Module ADDSTF
CmPurpose Assemble Global stiffness matrix
C=Author who knows
C=Update January 1989, by E. Pramono
C=Block Fortran
      subroutine ADDSTF(sk,lm,bk,jdiag,nseq)
C
      PURPOSE:
C
         THIS SUBROUTINE ASSEMBLES THE ELEMENT STIFFNESS MATRICES
                                                                          C
C
         INTO THE COMPACTED GLOBAL STIFFNESS VECTOR.
                                                                          C
C
      ARGUMENTS:
C
C
                                                                          C
             - ELEMENT STIFFNESS MATRIX
         sk
C
                                                                          C
               - LOCATION VECTOR FOR ELEMENT STIFFNESS MATRIX
         1m
C
                                                                          C
               - COMPACTED GLOBAL STIFFNESS VECTOR
C
         jdiag - VECTOR OF DIAGONAL ELEMENT ADDRESSES
                                                                         - C
C
         nseq - NUMBER OF DEGREES OF FREEDOM PER ELEMENT
                                                                          C
C.
C
    ARGUMENTS
      real*8 sk(nseq,nseq), bk(1)
      integer lm(18), jdiag(1)
integer lm(18), jdiag(1), nseq
C
C
    LOCAL ARGUMENTS
      integer i, j, k, l, m
    ASSEMBLE GLOBAL STIFFNESS AND LOAD ARRAYS
      do 20 j = 1, nseq
         k = lm(j)
```

if (k .eq. 0) goto 20

C

LOCAL VARIABLES

```
l = jdiag(k) - k
Ç
         l = jdiag(k+1) - k
         do 10 i = 1, nseq
            n = ln(i)
            if(m .gt. k .OR. m .eq. 0) goto 10
            m = 1 + m
            bk(m) = bk(m) + sk(i,j)
10
         continue
20
      continue
      return
      end
C=End Fortran
File: beam3d.f
C=Module BEAM3D
C=Purpose Construct 3-d Timoshenko beam element stiffness and lumped mass
C=Author K. Alvin
C=Date May 1990
C=Block Fortran
      subroutine BEAM3D(n,ni,nj,nk,xyz,emod,gmod,rho,area,ssf2,ssf3,
     Ł
                         jtor, i2, i3, ipin, sk, sm)
   ARGUMENTS:
C
C
                Element ID Number
        n
C
        ní
                Node ID Number at End i
C
        пj
                Node ID Number at End j
C
        XYZ
                Node Location Array
                Material Elastic Modulus (Young's Modulus)
C
        emod
C
                Material Modulus of Rigidity (Shear Modulus)
        gmod
C
        Tho
                Material Mass Density
C
        area
                Element Cross-sectional area
C
                Shear shape factor in element x2 direction
        ssf2
C
        ss13
                Shear shape factor in element x3 direction
C
        jtor
                Torsional constant J
C
        i2
                 Area moment of inertia about element x2 axis
C
        i3
                 Area moment of inertia about element x3 axis
C
                Pin release codes: O=Fixed, 1=Freed
        ipin
C
                 (1)
                         Axial
C
                 (2)
                         Torsional
C
                 (3)
                         End A rotation about x2 axis
C
                 (4)
                         End A rotation about x3 axis
C
                 (5)
                         End B rotation about x2 axis
C
                         End B rotation about x3 axis
                 (6)
C
                 Element Stiffness Matrix
        sk.
                 Element Mass Matrix
        SM
      integer n,ni,nj,nk,ipin(1)
      real*8 xyz(3,1),emod,gmod,rho,area,ssf2,ssf3,jtor,i2,i3
      real*8 sk(12,1),sm(12,1)
C LOCAL VARIABLES:
      integer i,j
      real*8 dc(3,3),length,rlength,kc(10),mc(3)
```

```
C LOGIC
    Find Element Length
      length = 0.0d0
      do 10 i * 1,3
        de(i,i) = xyz(i,nj) - xyz(i,ni)
        length = length + dc(1,i) + +2.
10
        continue
      length = sqrt(length)
      if (length .eq. 0.0d0) then
        print *, 'BAR2D: Zero element length; nz ',n
        return
        endif
    Find direction cosines for x1,x2,x3 element axes
      do 15 i=1,3
        dc(1,i) = dc(1,i)/length
        if (ak .eq. 0) then
          de(2,i) = 0.0
        else
          dc(2,i) = xyz(i,nk) - xyz(i,ni)
          endif
15
        continue
      if (nk \cdot eq. 0) dc(2,3) = 1.0
      dc(3,1) = dc(1,2)*dc(2,3) - dc(2,2)*dc(1,3)
16
      dc(3,2) = dc(2,1)*dc(1,3) - dc(1,1)*dc(2,3)
      dc(3,3) = dc(1,1)*dc(2,2) - dc(2,1)*dc(1,2)
      Flength * sqrt(dc(3,1)**2 + dc(3,2)**2 + dc(3,3)**2)
      if (rlength .ne. 0.) goto 17
      dc(2,2) = 1.0
      dc(2,3) = 0.0
      goto 16
17
      do 18 i=1,3
        dc(3,i) = dc(3,i)/rlength
18
        continue
      dc(2,1) = dc(3,2)*dc(1,3) - dc(1,2)*dc(3,3)
      dc(2,2) = dc(1,1)*dc(3,3) - dc(3,1)*dc(1,3)
      dc(2,3) = dc(3,1)*dc(1,2) - dc(1,1)*dc(3,2)
C Compute various stiffness constants, accounting for pin codes
      if (ipin(1) .eq. 0) them
        kc(1) = area = emod/length
      else
        kc(1) = 0.0d0
        endif
      if (ipin(4) .eq. 0) then
        if (ipin(6) .eq. 0) then
          kc(2) = area*gmod*ssf2/length
          kc(6) = i3*emod/length
          kc(7) = kc(2) + length/2.0d0
          kc(9) = kc(7) + length/2.0d0
```

print \*,'BEAM3D: Pin code error, x3 direction, el #',n

```
endif
else
  if (ipin(6) .eq. 0) then
    print *,'BEAM3D: Pin code error, x3 direction, el $',n
  else
    kc(2) = 0.0d0
    kc(6) = 0.040
    kc(7) = 0.0d0
    kc(9) = 0.0d0
    endif
  andif
if (ipin(3) .eq. 0) then
  if (ipin(5) .eq. 0) then
    kc(3) = area = gmod = saf3/length
    kc(5) = i2+emod/length
    kc(8) = kc(3) + length/2.0d0
    kc(10) = kc(8) + length/2.0d0
    print *,'BEAM3D: Pin code error, x2 direction, el #',n
    endif
else
  if (ipin(5) .eq. 0) then
    print *,'BEAM3D: Pin code error, x2 direction, el $',n
  else
    kc(3) = 0.0d0
    kc(5) = 0.0d0
    kc(8) = 0.0d0
    kc(10) = 0.0d0
    endif
  endif
if (ipin(2) .eq. 0) then
  kc(4) = jtor*gmod/length
else
  kc(4) = 0.0d0
  endif
mc(1) = area+rho+length/2.0d0
mc(2) = i2 + rho + length/2.0d0
mc(3) = i3*rho*length/2.0d0
sk(1,1)
          * kc(1)*dc(1,1)*dc(1,1) + kc(2)*dc(2,1)*dc(2,1) +
             kc(3)*dc(3,1)*dc(3,1)
sk(1,2)
             kc(1)+dc(1,1)+dc(1,2) + kc(2)+dc(2,1)+dc(2,2) +
             kc(3)*dc(3,1)*dc(3,2)
sk(1,3)
             kc(1)*dc(1,1)*dc(1,3) + kc(2)*dc(2,1)*dc(2,3) +
             kc(3)*dc(3,1)*dc(3,3)
sk(1,4)
             kc(7)*dc(2,1)*dc(3,1) - kc(8)*dc(3,1)*dc(2,1)
sk(1,5)
          * kc(7)*dc(2,1)*dc(3,2) - kc(8)*dc(3,1)*dc(2,2)
          \approx kc(7)*dc(2,1)*dc(3,3) - kc(8)*dc(3,1)*dc(2,3)
sk(1,6)
sk(1,7)
          = -sk(1,1)
sk(1,8)
          = -sk(1,2)
sk(1,9)
          = -sk(1.3)
sk(1,10)
             sk(1,4)
sk(1,11)
             sk(1,5)
sk(1,12)
             sk(1.6)
sk(2,2)
             kc(1)*dc(1,2)*dc(1,2) + kc(2)*dc(2,2)*dc(2,2) +
             kc(3)*dc(3,2)*dc(3,2)
```

```
kc(1)*dc(1,2)*dc(1,3) + kc(2)*dc(2,2)*dc(2,3) +
sk(2,3)
             kc(3)*dc(3,2)*dc(3,3)
sk(2,4)
             kc(7)*dc(2,2)*dc(3,1) = kc(8)*dc(3,2)*dc(2,1)
             kc(7)*dc(2,2)*dc(3,2) - kc(8)*dc(3,2)*dc(2,2)
sk(2,5)
sk(2,6)
             kc(7)*dc(2,2)*dc(3,3) \sim kc(8)*dc(3,2)*dc(2,3)
sk(2,7)
          = -sk(1.2)
          = -sk(2,2)
sk(2,8)
sk(2,9)
          s -sk(2,3)
sk(2,10)
             sk(2,4)
sk(2,11)
             sk(2,5)
sk(2,12)
             sk(2.6)
sk(3,3)
             kc(1)*dc(1,3)*dc(1,3) + kc(2)*dc(2,3)*dc(2,3) +
             kc(3)*dc(3,3)*dc(3,3)
sk(3,4)
             kc(7)*dc(2,3)*dc(3,1) \sim kc(8)*dc(3,3)*dc(2,1)
             kc(7)*dc(2,3)*dc(3,2) - kc(8)*dc(3,3)*dc(2,2)
sk(3,5)
sk(3,6)
             kc(7)*dc(2,3)*dc(3,3) - kc(8)*dc(3,3)*dc(2,3)
sk(3.7)
          = -sk(1,3)
sk(3,8)
          s - sk(2,3)
sk(3,9)
          = -sk(3,3)
sk(3,10)
             sk(3,4)
sk(3,11)
             sk(3,5)
sk(3,12)
             sk(3,6)
sk(4,4)
             kc(4)*dc(1,1)*dc(1,1)+(kc(10)+kc(5))*dc(2,1)*dc(2,1)
             + (kc(9)+kc(6))*dc(3,1)*dc(3,1)
sk(4,5)
             kc(4)*dc(1,1)*dc(1,2)+(kc(10)+kc(5))*dc(2,1)*dc(2,2)
             + (kc(9)+kc(6))+dc(3,1)+dc(3,2)
sk(4,6)
             kc(4)*dc(1.1)*dc(1.3)*(kc(10)*kc(5))*dc(2.1)*dc(2.3)
             + (kc(9)+kc(6))*dc(3,1)*dc(3,3)
sk(4,7)
          = -sk(1,4)
sk(4,8)
          = -sk(2,4)
          = -sk(3,4)
sk(4,9)
sk(4,10)
          = -kc(4)*dc(1,1)*dc(1,1)*(kc(10)-kc(5))*dc(2,1)*dc(2,1)
             + (kc(9)-kc(6))*dc(3,1)*dc(3,1)
          = -kc(4)*dc(1,1)*dc(1,2)+(kc(10)-kc(5))*dc(2,1)*dc(2,2)
sk(4,11)
             + (kc(9)-kc(6))+dc(3,1)+dc(3,2)
          = -kc(4)*dc(1,1)*dc(1,3)+(kc(10)-kc(5))*dc(2,1)*dc(2,3)
sk(4,12)
             + (kc(9)-kc(6))*dc(3,1)*dc(3,3)
sk(5.5)
          = kc(4)*dc(1,2)*dc(1,2)+(kc(10)+kc(5))*dc(2,2)*dc(2,2)
             + (kc(9)+kc(6))+dc(3,2)+dc(3,2)
sk(5,6)
             kc(4)*dc(1,2)*dc(1,3)+(kc(10)+kc(5))*dc(2,2)*dc(2,3)
             + (kc(9)+kc(6))+dc(3,2)+dc(3,3)
sk(5,7)
          = -sk(1,5)
sk(5,8)
          = -sk(2,5)
          = -sk(3,5)
sk(5,9)
sk(5,10)
          = sk(4,11)
sk(5,11)
          = -kc(4)*dc(1,2)*dc(1,2)+(kc(10)-kc(5))*dc(2,2)*dc(2,2)
             + (kc(9)-kc(6))+dc(3,2)+dc(3,2)
          = -kc(4)*dc(1,2)*dc(1,3)+(kc(10)-kc(5))*dc(2,2)*dc(2,3)
sk(5,12)
             + (kc(9)-kc(6))*dc(2,3)*dc(3,3)
sk(6,6)
             kc(4)*dc(1.3)*dc(1.3)*(kc(10)*kc(5))*dc(2.3)*dc(2.3)
             + (kc(9)+kc(6))*dc(3,3)*dc(3,3)
sk(6,7)
          = -sk(1,6)
sk(6,8)
          = -sk(2.6)
          = -sk(3,6)
sk(6,9)
sk(6,10)
             sk(4,12)
sk(6,11)
             sk(5,12)
sk(6,12)
            -kc(4)*dc(1,3)*dc(1,3)+(kc(10)-kc(5))*dc(2,3)*dc(2,3)
             + (kc(9)-kc(6))*dc(3,3)*dc(3,3)
sk(7,7)
          = sk(1,1)
```

```
sk(1,2)
      sk(7.8)
      sk(7,9)
                    sk(1,3)
      sk(7,10)
                   -sk(1,4)
      sk(7,11)
                   -sk(1.5)
      sk(7,12)
                   -sk(1,6)
      sk(8,8)
                    sk(2,2)
                    sk(2,3)
      sk(8,9)
      sk(8,10)
                   -sk(2,4)
      sk(8,11)
                 s -sk(2,5)
      sk(8,12)
                   -sk(2,6)
      sk(9,9)
                    sk(3,3)
      sk(9,10)
                 = -sk(3,4)
      sk(9,11)
                 = -sk(3,5)
      sk(9,12)
                   -sk(3,6)
      sk(10,10) =
                    sk(4,4)
      sk(10,11)
                    sk(4,5)
      sk(10,12) =
                    sk(4,6)
      sk(11,11) =
                    sk(5,5)
      sk(11,12) =
                    sk(5,6)
      sk(12,12) = sk(6,6)
      do 50 i = 1,12
        do 55 j = 1,12
           sm(i,j) = 0.d0
55
           continue
50
         continue
   Row-sum rotated mass matrix to re-diagonalize
      sm(1,1)
                    mc(1)
      sm(2,2)
                    mc(1)
      sm(3,3)
                    mc(1)
```

```
sm(4,4)
                   mc(2)*(dc(1,1)*dc(1,1)+dc(2,1)*dc(2,1))
                    mc(3)*(dc(1,1)*dc(1,1)+dc(3,1)*dc(3,1))
                    mc(2)*(dc(1,1)*dc(1,2)+dc(2,1)*dc(2,2))
                    mc(3)*(dc(1;1)*dc(1,2)+dc(3,1)*dc(3,2))
                    mc(2)*(dc(1,1)*dc(1,3)+dc(2,1)*dc(2,3))
                    mc(3)*(dc(1,1)*dc(1,3)+dc(3,1)*dc(3,3))
C
      sm(4,5)
                  mc(2)*(dc(1,1)*dc(1,2)+dc(2,1)*dc(2,2))
C
                    mc(3)*(dc(1,1)*dc(1,2)+dc(3,1)*dc(3,2))
C
      sm(4,6)
                   mc(2)*(dc(1,1)*dc(1,3)+dc(2,1)*dc(2,3))
C
                    mc(3)*(dc(1,1)*dc(1,3)+dc(3,1)*dc(3,3))
C
                   mc(2)*(dc(1,1)*dc(1,2)+dc(2,1)*dc(2,2))
      sm(5,4)
C
                    mc(3)*(dc(1,1)*dc(1,2)+dc(3,1)*dc(3,2))
      sm(5,5)
                   mc(2)*(dc(1,2)*dc(1,2)+dc(2,2)*dc(2,2))
                   mc(3)*(dc(1,2)*dc(1,2)*dc(3,2)*dc(3,2))
                   mc(2)*(dc(1,1)*dc(1,2)+dc(2,1)*dc(2,2))
                    mc(3)*(dc(1,1)*dc(1,2)+dc(3,1)*dc(3,2))
                    mc(2)*(dc(1,2)*dc(1,3)+dc(2,2)*dc(2,3))
                    mc(3)*(dc(1,2)*dc(1,3)+dc(3,2)*dc(3,3))
C
      sm(5,6)
                   mc(2)*(dc(1,2)*dc(1,3)+dc(2,2)*dc(2,3))
C
                    mc(3)*(dc(1,2)*dc(1,3)+dc(3,2)*dc(3,3))
C
      sm(6,4)
                   mc(2)*(dc(1,1)*dc(1,3)+dc(2,1)*dc(2,3))
C
                    mc(3)*(dc(1,1)*dc(1,3)+dc(3,1)*dc(3,3))
C
      sm(6,5)
                   mc(2)*(dc(1,2)*dc(1,3)+dc(2,2)*dc(2,3))
                    mc(3)*(dc(1,2)*dc(1,3)+dc(3,2)*dc(3,3))
      sm(6,6)
                   mc(2)*(dc(1,3)*dc(1,3)+dc(2,3)*dc(2,3))
                    mc(3)*(dc(1,3)*dc(1,3)+dc(3,3)*dc(3,3)) +
```

```
mc(2)*(dc(1,1)*dc(1,3)*dc(2,1)*dc(2,3)) +
                   mc(3)*(dc(1,1)*dc(1,3)+dc(3,1)*dc(3,3)) +
                   mc(2)*(dc(1,2)*dc(1,3)+dc(2,2)*dc(2,3)) +
                   mc(3)*(dc(1,2)*dc(1,3)+dc(3,2)*dc(3,3))
      sa(7,7)
                   mc(1)
      sæ(8,8)
                   mc(1)
                   mc(1)
      sm(9,9)
      sm(10,10) =
                   sm(4,4)
C
      sm(10,11) =
                   sm(4,5)
C
      sm(10,12) s
                   SE (4,6)
C
      sm(11,10) =
                   sm(5,4)
      em(11,11) =
                   am(5,5)
C
      sm(11,12) s
                   sm(5,6)
C
      sm(12,10) =
                   sm(6,4)
C
      sm(12,11) =
                   sm(6,5)
      sm(12,12) =
                   sm(6,6)
      do 100 i=1,12 '
        do 200 j=1,i-1
          sk(i,j) = sk(j,i)
200
          continue
100
        continue
      return
      end
C=End Fortran
File: forces.f
C=Module FORCES
C=Purpose Calculate applied force vector at given time
C=Author K. Alvin
C=Date May 1990
C=Block Fortran
C
      Subroutine FORCES
C
C
      Purpose:
C
         Returns force from stored function at any given time.
C
         The forcing functions are hardwired by the user. The
C
         function is selectable at program excecution using the
C
         forcing function ID, which by convention is the statement
Ç
         label used in branching.
C
C
      subroutine FORCES(time)
      include 'shared.inc'
      real*8 time,pi
C
      LOGIC
      pi = 3.1415926
```

```
call ZEROVECT(f,ndof)
 101
       if (forceid .eq. 101) then
         if (time .1e. .02) then
           1(id(2,15)) = 100.*(1.-cos(2.*pi*time/.02))
         endif
 102
       elseif (forceid .eq. 102) then
         if (time .lt. .1) then
           1(id(2,95)) = 10.
         elseif (time .eq. .1) then
           1(id(2,95)) = 0.
         elseif ((time .gt. .1).and.(time .lt. .2)) then
           f(id(2,95)) = -10.
         else
           f(id(2,95)) = 0.
         endif
. 103
       elseif (forceid .eq. 103) then
         if (time .le. .01) then
           f(id(1,15)) = 100
         endif
 104
       elseif (forceid .eq.104) then
         if ((time .gt. 0) .and. (time .lt. .17)) then
            f(id(3,125)) = 10
         elseif ((time .gt. .17) .and. (time .lt. 1.0)) then
            1(id(3,125)) = -10
         endif
 105 elseif (forceid .eq. 105) then
         if (time .le. .01) then
           f(id(2,9)) = 100.*(1.-cos(2.*pi*time/.01))
         elseif (time .le. .02) then
           f(id(2,9)) = 100.*(cos(2.*pi*time/.01)-1.)
         endif
       endif
       do 10 i = 1, ndof
         f(i) = scalef + f(i)
- 10
       continue
       return
       end
```

## File: input.f

C=Module IMPUT
C=Purpose Input data parameters for ACSIS
C=Author K. Alvin

```
C=Date May 1990
C=Block Fortran
C
C
      Subroutine INPUT
C
C
C
C
C
    Argument definitions
C
C
      runtype - ID of analysis run type
C
      aavin
               - variable to control creation of input file
C
      runfile - variable indicates if run is from input file
C
      comment - dummy name for comment input lines
      outskip - number of steps to skip before sending output
      subroutine INPUT(runtype,outskip)
      include 'shared.inc'
      integer runtype, outskip
      character *1 savin, runfile, temp
      character#48 comment, inpfile
C
      PRINT AND READ START-UP
      print *, '2nd Order Accelerated CSI Simulation (ACSIS)'
      print *
      print *, 'Please input analysis type:'
      print *
      print *, '
                    1. Eigenmode Analysis'
      print *, '
                   2. CSI Simulation'
      print *, ' 3. Transient Response'
      print *
      read *, runtype
      RUN OPTIONS AND INPUT FILE SETUP
      runfile = 'n'
      if (runtype .lt. 0) then
         runtype = -1 * runtype
         runfile = 'y'
      print *, 'Do you wish to save an input file? (y or n)'
      read 21, savin
20
      format (a32)
      format (a1)
21
      if (savin .eq. 'y') then
         print *, 'Name of save input file? (filename)'
         read 20, inpfile
         open(16,file=inpfile)
         runtype = -1 * runtype
         write(16,'(i2)') runtype
        runtype = -1 * runtype
         write(16,'(a1)') 'n'
         write(16,'(a47)') '* ACSIS input file, two lines above are'
         write(16,'(a48)') '* analysis type and save input file. Do'
         write(16,'(a48)') '* not change them by editing this file.'
      endif
```

```
runtype = runtype - 2
      if (runfile .eq. 'y') then
         do 30 i = 1.4
            read 20, comment
30
         continue
      endif
      print *, 'Finite Element Model Input File Name (filename)'
      read 20, femfile
      open(11,file=femfile)
      if (savin .eq. 'y') then
        write(16,'(a47)') '* Finite element input file?(filename)'
        write(16,'(a32)') femfile
      endif
      if (runtype) 100,200,300
      EIGENMODE INPUTS
      print *, 'Number of modes desired:'
100
      if (runfile .eq. 'y') read 20, comment
      read *, neig
      if (runfile .eq. 'y') read 20, comment
      print *, 'Output File Name:'
      read 20, outfile
      open(13,file=outfile)
      if (savin .eq. 'y') then
        write(16,'(a35)') '* Number of modes desired?'
       write(16,'(i4)') neig write(16,'(a33)') '* Output file?(filename)'
        write(16,'(a32)') outfile
      endif
      call READFEM
      goto 1000
      CSI INPUTS
      print *. 'Controller Definition File Name:'
      if (runfile .eq. 'y') read 20, comment
      read 20, confile
      open(12,file=confile)
      print *, 'Please input type of control:'
      print *
      print *, '
                    1. Full State Feedback'
      print *, '
                    2. Luenberger Observer (L1=0)'
      print *, '
                    3. Kalman Filter'
      print *
      if (runfile .eq. 'y') read 20, comment
      read *, contype
      contype = contype - 2
      print *,'Initial time, final time, control-on time, step size:'
      if (runfile .eq. 'y') read 20, comment
      read *, t0,tf,tc,h
      print *,'Forcing function ID, scale factor, damping coeff- a,b:'
      if (runfile .eq. 'y') read 20, comment
      read *, forceid, scalef, adamp, bdamp
      print *,'Phase lag fix?(y or n):'
      if (runfile .eq. 'y') read 20, comment
```

```
read 21, temp
if (temp .eq. 'y') nolag = .true.
if (temp .eq. 'n') nolag = .false.
print *,'Gain scale factors (4 total):'
if (runfile .eq. 'y') read 20, comment
read *, qalpha, qbeta, qalphao, qbetao
if (savin .eq. 'y') then
  write(16,'(a42)') '* Controller file name?(filename)'
  write(16,'(a32)') confile
  write(16,'(a42)') '* Please input type of control: '
  write(16,'(110)') contype + 2
  write(16,'(a46)') '* Initial, final, control-on, step size?'
  write(16,'(4f14.8)') t0,tf,tc,h
  write(16,'(a49)') '* Forcing function, scale f, damping a,b?'
  write(16,'(i4,f15.6,2f12.8)') forceid,scalef,adamp,bdamp
  write(16,'(a32)') '* Phase lag fix?(y or n)'
  if (nolag) write(16,'(a1)') 'y'
  if (.not. nolag) write(16,'(a1)') 'n'
 Write(16,'(a40)') '* Gain scale factors (4 total)?'
  write(16,'(4f14.8)') qalpha,qbeta,qalphao,qbetao
endif
call READFEM
goto 999
TRANSIENT RESPONSE INPUTS
print *,'Initial time, final time, step size:'
if (runfile .eq. 'y') read 20, comment
read *, t0,tf,h
print *, 'Forcing function ID, scale factor, damping coeff- a,b:'
if (runfile .eq. 'y') read 20, comment
read *, forceid, scalef, adamp, bdamp
if (savin .eq. 'y') then
  write(16,'(a48)') '* Initial, final, step size?'
  write(16,'(3f14.8)') t0,tf,h
  write(16,'(a49)') '* Forcing function, scale f, damping a,b?'
  write(16,'(i4,f15.6,2f12.8)') forceid,scalef,adamp,bdamp
endif
call READFEM
goto 999
OUTPUT OPTIONS
print *, 'Output File Name:'
if (runfile .eq. 'y') read 20, comment
read 20, outfile
open(13,file=outfile)
print *,'Number of displacement results to output (max 10):'
if (runfile .eq. 'y') read 20, comment
read *,ndisout
do 500 i=1,ndisout
  print *,'Input node *, dof for displacement output*',i
  read *,outlabel(i),outlabel(i+10)
print *,'Number of velocity results to output (max 10):'
```

300

999

500

```
if (runfile .eq. 'y') read 20, comment
      read *.nvelout
      do 600 i=1,nvelout
        print *,'Input node $, dof for velocity output#',i
        read *,outlabel(i+20),outlabel(i+30)
600
      continue
      print *,'Send output every how many steps?'
      if (runfile .eq. 'y') read 20, comment
      read *, outskip
      if (savin .eq. 'y') then
        write(16,'(a38)') '* Output file name?(filename)'
        write(16,'(a32)') outfile
        write(16,'(a42)') '* Number of displacement outputs?'
        write(16,'(14)') ndisout
        do 650 i=1,ndisout
           write(16,'(2i8)') outlabel(i),outlabel(i+10)
650
        continue
        write(16,'(a38)') '* Number of velocity outputs?'
        write(16,'(14)') arelout
        do 660 i=1,nvelout
           write(16,'(218)') outlabel(i+20),outlabel(i+30)
660
        write(16,'(a44)') '* Send output every how many steps?'
        write(16,'(i3)') outskip
      endif
C
      ANIMATION OPTION
      print *,'Animation Output? (y or n):'
      if (runfile .eq. 'y') read 20, comment
      read 21, temp
      if (temp .eq. 'y') animate = .true.
      if (temp .eq. 'n') animate = .false.
      if (animate) then
        print*,'Animation file name (filename)'
        if (runfile .eq. 'y') read 20, comment
        read 20, animfile
        open (15, file=animfile)
      endif
      if (savin .eq. 'y') then
        write(16,'(a41)') '* Send animation output?(y or n)'
        if (animate) write(16,'(a1)') 'y'
        if (.not. animate) write(16,'(a1)') 'n'
        if (animate) then
          write(16,'(a31)') '* Animation file name?'
          write(16,'(a32)') animfile
        andif
      endif
      delta = h/2.
      delsq = delta**2
1000 return
      end
```

File: pmvmul.f

```
C=Hodule PHYHUL
CaAuthor K. Alvin
CaDate May 1990
CaBlock Portran
C
      Subroutine PMVMUL
C
      Purpose:
C
        This subroutine multiplies a matrix in vector form
C
        and a vector.
C
C
C
      Arguments
C
        á
                  matrix in vector form
C
                  Vector
C
                  result vector
C
        Req
               - order of vector and square matrix
C
        jdiag - array of diagonal addresses for a
      subroutine PMVMUL(a,jdiag,b,neq,c)
      recursive subroutine PMVMUL(a,jdiag,b,neq,c)
      real=8 a(1), b(1), c(1)
      integer jdiag(1), neq
      do 100 i=1,neq
        c(i) = a(jdiag(i))*b(i)
100
      continue
      do 200 i=2,neq
        do 300 j=jdiag(i-1)+1,jdiag(i)-1
          k = jdiag(i) - j
          c(i) = c(i) + a(j)*b(i-k)
300
        continue
200
      continue
      do 250 i=2,neq
        do 400 j=jdiag(i-1)+1,jdiag(i)-1
          k = jdiag(i) - j
          c(i-k) = c(i-k) + a(j)*b(i)
400
        continue
250
      continue
      return
      end
C
C
C
C
      Subroutine PMVMAD
C
      Purpose:
        Multiply a matrix in vector form and a vector and add the
        resultant vector multiplied by a constant to a second vector
```

```
C
        multiplied by a second vector
Ç
C
C
C
      Arguments
C
                 matrix in vector form
        .
C
        Ъ
                 vector to be multiplied with matrix
C
               - resultant and vector to be added
C
        fact1 - constant multiplier of matrix and first vector
C
        fact2 - constant multiplier of second vector
C
                  array of diagonal addresses for matrix
        jdiag -
C
                  order of vectors and matrix
C
C
      subroutine PMVMAD(a,jdiag,b,neq,fact1,c,fact2)
      recursive subroutine PMVMAD(a,jdiag,b,neq,fact1,c,fact2)
      real=8 a(1), b(1),c(1),fact1,fact2
      integer jdiag(1), neq
      do 100 i=1,neq
        c(i) = fact2*c(i) + fact1*a(jdiag(i))*b(i)
-100
      continue
      do 200 i=2,neq
        do 300 j=jdiag(i-1)+1,jdiag(i)-1
          k = jdiag(i) - j
          c(i) = c(i) + facti*a(j)*b(i-k)
300
          continue
200
      continue
      do 250 i=2,neq
        do 400 j=jdiag(i-1)+1,jdiag(i)-1
          k = jdiag(i) - j
          c(i-k) = c(i-k) + facti+a(j)+b(i)
400
          continue
250
      continue
      return
      end
File: prepfem.f
```

```
C=Module PREPFEM
C=Purpose Preprocess Structure Finite Element module for ACSIS
C=Author K. Alvin
C=Date May 1990
C=Block Fortran
C
C
C
Subroutine PREPFEM
C
C
C
Purpose:
C
This subroutine prepares the finite element mass,
Stiffness, and S matrices in reduced profile vector form
```

```
C
C
C
Ç
      Local variables:
C
C
        sk
                Element Stiffness matrix
C
                Element Mass Matrix
        8 M
C
        lm
                Local/Global DOF Mapping vector
C
                Number of element degrees of freedom
C
                Material and Propety id $ for element
       em, ep
      subroutine PREPFEM
      include 'shared.inc'
   LOCAL VARIABLES
      parameter (MAISEQ=24)
      real+8 sk(MAYSEQ, MAISEQ), sm(MAISEQ, MAISEQ), mc, kc
      integer lm(MAXSEQ), nseq, em, ep
      call RENUM
   Set up skyline storage profile for global matrices
      call PROFILE(ix,id,jdiag,nnp,nel,4,6,mlen,ndof,mask)
   Perform automatic domain decomposition
      call DOMDEC
  Check size of skyline profile against storage limitation
      if (mlen .gt. MAXMLEN) then
       print*, 'PREPFEM: error, global matrix exceeded max. size'
      endif
  Zero Global Matrices prior to assembly
      call ZEROVECT(stif,mlen)
      call ZEROVECT(mass,mlen)
    ASSEMBLE EACH ELEMENT MASS AND STIFFNESS
      do 100 n=1.nel
        do 20 k=1.4
          j=ix(k,n)
          if ((etype(n).eq.1).and.(k.gt.2)) j = 0
          do 30 i=1,6
            kk=6*(k-1) + i
            if (j .ne. 0) then
              lm(kk) = id(i,j)
            else
              lm(kk) = 0
               endif
30
            continue
```

20

continue

```
if (etype(n) .eq. 1) then
         nseq = 12
          em = emat(n)
         ep = eprop(n)
          call BEAM3D(n,ix(1,n),ix(2,n),ix(3,n),coxyz,mat(1,em),
              mat(2,em),mat(3,em),prop(1,ep),prop(5,ep),prop(6,ep),
              prop(2,ep),prop(3,ep),prop(4,ep),pin(1,n),sk,sm)
        elseif (ix(1,n) .ne. 0) then
     print+, 'PREPFEM: Element type not found, n=',n,'etype=',etype(n)
        endif
   ADD ELEMENT TO GLOBAL MASS AND STIFFNESS
        call ADDSTF(sk,lm,stif,jdiag,nseq)
        call ADDSTF(sm,lm,mass,jdiag,nseq)
    SAVE THE ELEMENT STIFFNESS FOR E-BY-E COMPUTATIONS
     call SAVESK(sk.n.nseq)
100
        continue
    ADD LUMPED INERTIAS TO GLOBAL MASS#
     do 125 i=1,nnp
        do 130 j=1,6
          if (id(j,i) .eq. 0) goto 130
          k=jdiag(id(j,i))
          mass(k) = mass(k) + inertia(j,i)
130
          continue
        continue
125
    ASSEMBLE AND FACTORIZE es (S MATRIX)
      mc = 1. + delta * adamp
      kc = delta*bdamp + delsq
      do 200 i=1,mlen
        es(i) = mc*mass(i) + kc*stif(i)
200
        continue
      call SOLVER(es,gs,jdiag,ndof,1)
    INITIALIZE DISPLACEMENT AND VELOCITY VECTORS
C
      do 300 i = 1, nnp
        do 350 j = 1,6
          if (id(j,i) .ne. 0) then
            q(id(j,i)) = q0(j,i)
            qdot(id(j,i)) = qdot0(j,i)
            endif
350
          continue
300
        continue
      return
      end
      subroutine SAVESK(sk,n,nseq)
      include 'shared.inc'
```

```
real*8 sk(nseq,1)
      integer n,nseq
      k=0
      do 10 j=1,nseq
        de 20 i=1,j
          kek+1
          estifm(k,n)=sk(i,j)
20
          continue
10
        continue
      return
      end
      subroutine DOMDEC
      include 'shared.inc'
      logical nchk,ndchk(MAXNODE,MAXDOM)
      integer ndom
      do 10 j=1,MAXDON
        neld(j)=0
        de 20 is1,mp
          ndchk(i,j)=.false.
20
          continue
10
        continue
      ndomain=0
      do 100 n=1,nel
        ndom=0
        nchk=0
        do 200 while (nchk.eq.0)
          ndom=ndom+1
          if (ndom.gt.ndomain)- ndomain=ndom
          nchk=1
          if (ndchk(ix(1,n),ndom,) nchk=0
          if (ndchk(ix(2,n),ndom)) nchk=0
          if (nchk.eq.1) then
            eldom(n)=ndom
            ndchk(ix(1,n),ndom)=.true.
            ndchk(ix(2,n),ndom)=.true.
            endif
200
          continue
        neld(ndom)=neld(ndom)+1
        elnum(neld(ndom),ndom)=n
100
        continue
      return
      end
```

File: profile.f

```
C=Module PROFILE
C=Purpose Compute the number of equations and set profile for K
C=Author Bob Taylor
C=Date who knows
CsUpdate January 1989 by E. Pramono
C=Block Fortran
      subroutine PROFILE(ix,id,jdiag,nnp,nel,nen,ndof,nad,neq,mask)
C+
. C
      PURPOSE:
                                                                         C
C
          THIS SUBROUTINE COMPUTES THE NUMBER OF EQUATIONS REQUIRED
                                                                         C
C
          TO SOLVE THE PROBLEM BY ELIMINATING RESTRAINED DEGREES OF
                                                                         C
C
          FREEDOM FROM THE SYSTEM OF EQUATIONS. KNOWING THE EQUATION
                                                                         C
C
                                                                         C
         NUMBERS COORESPONDING TO THE NODAL DEGREES OF FREEDOM, THE
C
                                                                         C
       DIAGONAL ELEMENT LOCATIONS CAN BE COMPUTED FOR STORING THE
C
                                                                         C
          GLOBAL STIFFNES MATRIX IN COMPACTED VECTOR FORM.
C-
C
C
    ARGUNENTS
C
      integer ix(nen,1), id(ndof,1), jdiag(1)
      integer nnp, nel, nad, neq, mask(1)
C
      integer nnp, nel, nen, ndof, nad, neq, mask(1)
C
    LOCAL ARGUMENTS
C
       integer i, j, k, 1, m, n, j1, k1, l1, m1
    SET UP EQUATION NUMBERS
      neq = 0
      do 30 n = 1, nnp
          do 20 m = 1, ndof
            j = id(m, mask(n))
            if (j .eq. 1) goto 10
            neq = neq + 1
            id(m,mask(n)) = neq
            jdiag(neq) = 0
            goto 20
10
             id(m,mask(n)) = 0
20
          continue
30
       continue
C
C
C
    COMPUTE COLUMN HEIGHTS
·C
      do 80 n = 1, nel
          do 70 m = 1, nen
            mi = ix(m,n)
             if (m1 .le. 0) goto 70
             do 60 1 = 1, ndof
                11 = id(1,m1)
                if (11 .eq. 0) goto 60
                do 50 k = m, nen
                   k1 = ix(k,n)
                   if (k1 .le. 0) goto 50
                   do 40 j = 1, ndof
                      j1 = id(j,k1)
                      if (j1 .eq. 0) goto 40
```

```
i = MAXO(11,j1)
                      jdiag(i) = MAXO(jdiag(i), IABS(l1-j1))
40
                  continue
50
               continue
60
            continue
70
         continue
80
      continue
C
C
C
    COMPUTE DIAGONAL POINTERS
      nad = 1
      jdiag(1) = 1
      if (meq .eq. 1) return
      do 90 n = 2, neq
         jdiag(n) = jdiag(n) + jdiag(n-1) + 1
90
      continue
      nad = jdiag(neq)
C
      return
      end
C=End Fortran
File: read.f
C=Module READ
C=Author K. Alvin
C=Date May 1990
C=Block Fortran
     Subroutine READFEN
C
C
      Purpose:
C.
        This subroutine reads the data file for the finite
C
      . element model.
C
C.
C
C
      Arguments
C
        ctype - stores code for type of line
      subroutine READFEM
C
      GLOBALS
      include 'shared.inc'
      LOCALS
      integer j,n,ctype,GETTYPE
      character *132 aline
      real*8 in
C
      INITIALIZE SIZE OF PROBLEM
```

```
nnp = 0
      nel = 0
      ndof = 0
      ndomain = 0
C
      IDENTIFY CARD TYPE AND ASSIGN INPUT
10
      read(11,1000,end=9999) aline
100
      ctype = GETTYPE(aline)
      if (ctype) 10,10,150
150
      if (aline(1:4) .eq. 'NODE') goto 200
      if (aline(1:4) .eq. 'TOPO') goto 300
      if (aline(1:4) .eq. 'ATTR') goto 400
      if (aline(1:4) .eq. 'MATE') goto 500
      if (aline(1:4) .eq. 'PROP') goto 600
      if (aline(1:4) .eq. 'FIXI') goto 700
      if (aline(1:4) .eq. 'INIT') goto 800
      if (aline(1:4) .eq. 'INER') goto 900 .
      if (aline(1:4) .eq. 'END ') goto 10
      if (aline(1:4) .eq. 'MESH') goto 10
      print *, 'READFEM: Unrecognized card type; ',aline(1:4)
      goto 10
C
      READ NODES
200
      read(11,1000,end=9999) aline
      ctype = GETTYPE(aline)
      if (ctype) 200,250,100
      read(aline,*) n,(coxyz(j,n),j=1,3)
250
      if (n .gt. nnp) nnp = n
      goto 200
C
      READ TOPOLOGY
300
      read(11,1000,end=9999) aline
      ctype = GETTYPE(aline)
      if (ctype) 300,350,100
350
      read(aline,*) n,etype(n),(ix(j,n),j=1,4)
      if (n . gt. nel) nel = n.
      goto 300
C
      READ ATTRIBUTES
      read(11,1000,end=9999) aline
400
      ctype = GETTYPE(aline)
      if (ctype) 400,450,100
450
      read(aline,*) n,emat(n),eprop(n),(pin(j,n),j=1,6)
      if (eldom(n).gt.ndomain) ndomain=eldom(n)
      goto 400
C
      READ MATERIAL
500
      read(11,1000,end=9999) aline
      ctype = GETTYPE(aline)
      if (ctype) 500,550,100
550
      read(aline,*) n,(mat(j,n),j=1,3)
      goto 500
```

C

READ PROPERTIES

```
600
      read(11,1000,end=9999) aline
      ctype = GETTYPE(aline)
      if (ctype) 600,650,100
650
      read(alize, *) n, (prop(j, n), j=1,6)
      goto 600
C
      READ FIXITY
700
      read(11,1000,end=9999) aline
      ctype = GETTYPE(aline)
      if (ctype) 700,750,100
750
      read(aline,*) n,(id(j,n),j=1,6)
      goto 700
      READ INITIAL CONDITIONS
800
      read(11,1000,end=9999) aline
      ctype = GETTYPE(aline)
      if (ctype) 800,850,100
850
      read(aline,*) n,j,q0(j,n),qdot0(j,n)
      goto 800
C
      READ INERTIA
900
      read(11,1000,end=9999) aline
      ctype = GETTYPE(aline)
      if (ctype) 900,950,100
      read(aline, *) n,j,in
950
      inertia(j,n)=inertia(j,n)+in
      goto 900
1000 format(a132)
9999 continue
      return
      end
C
C
C
C
      Subroutine READCON
C
C
      Purpose:
C
        This subroutine reads the actuator and sensor
C
        locations and the gains for the control system
C
C
C
C
      Arguments
C
        ctype - stores code for type of line
C
C
C
      Abbreviations
C
        NACT - number of actuators
        NSEN - number of sensors
C
C
        BMAT - locations of actuators
C
        HDMA - array of displacement sensor locations
        HVMA - array of velocity sensor locations
C
        PIGA - control gain matrix
```

```
C
        F2GA -
                 control gain matrix
        LIGA - state estimator filter gain matrix
        L2GA
                 state estimator filter gain matrix
      subroutine READCON
      include 'shared.inc'
C
      LOCALS
      real+8 val
      integer j,n,ctype,GETTYPE
      character *132 aline
      bval = 0
      hdval = 0
      hwwal = 0
      hdbval = 0
      hybral = 0
      IDENTIFY CARD TYPE AND ASSIGN INPUT
10
      read(12,1000,end=9999) aline
100
      ctype = GETTYPE(aline)
      if (ctype) 10,10,150
150
      if (aline(1:4) .eq. 'NACT') goto 200
      if (aline(1:4) .eq. 'NSEN') goto 300
      if (aline(1:4) .eq. 'BMAT') goto 400
      if (aline(1:4) .eq. 'HDMA') goto 500
      if (aline(1:4) .eq. 'HVMA') goto 600
      if (aline(1:4) .eq. 'F1GA') goto 700
      if (aline(1:4) .eq. 'F2GA') goto 800
      if (aline(1:4) .eq. 'L2GA') goto 900
      if (aline(1:4) .eq. 'L1GA') goto 1100
      if (aline(1:4) .eq. 'END ') goto 10
      print *,'READCON: Unrecognized card type; ',aline(1:4)
      goto 10
      READ INPUT CARDS
200
      read(12,1000,end=9999) aline
      ctype = GETTYPE(aline)
      if (ctype) 200,250,100
250
      read(aline,*) nact
      goto 200
300
      read(12,1000,end=9999) aline
      ctype = GETTYPE(aline)
      if (ctype) 300,350,100
350
      read(aline,*) nsen
      goto 300
400
      read(12,1000,end=9999) aline
      ctype = GETTYPE(aline)
      if (ctype) 400,450,100
      read(aline,*) i,j,n,val
450
      bval = bval + 1
      b(bval) = val
      brow(bwal) = id(j,i)
```

```
bcol(bval) = n
       goto 400
 500
       read(12,1000,end=9999) aline
       ctype = GETTYPE(aline)
       if (ctype) 500,550,100
 550
       read(aline,*) i,j,n,val
       hdval = hdval + 1
       hd(hdval) = val
       hdrow(hdwal) = n
       hdcol(hdval) = id(j,i)
       geto 500
 600
       read(12,1000,end=9999) aline
       ctype = GETTYPE(aline)
       if (ctype) 600,650,100
       read(aline, *) i, j, n, val
 650
       hvval = hvval + 1
       hv(hvval) = val
       hwrow(hwwal) = n
       hvcol(hvval) = id(j,i)
       goto 600
 700
       read(12,1000,end=9999) aline
       ctype = GETTYPE(aline)
       if (ctype) 700,750,100
       read(aline,*) i,j,n,val
 750
       f1(n,id(j,i)) = qalpha*val
       goto 700
 800
       read(12,1000,end=9999) aline
       ctype = GETTYPE(aline)
       if (ctype) 800,850,100
 850
       read(aline, *) i, j, n, val
       12(n,id(j,i)) = qbeta*val
       goto 800
 900
       read(12,1000,end=9999) aline
       ctype = GETTYPE(aline)
       if (ctype) 900,950,100
 950
       read(aline, *) i, j, n, val
       12(id(j,i),n) = qbetao*val
       goto 900
1100 read(12,1000,end=9999) aline
       ctype = GETTYPE(aline)
       if (ctype) 1100,1150,100
 1150 read(aline,*) i,j,n,val
       l1(id(j,i),n) = qalphao*val
       goto 1100
 1000 format(a132)
 9999
       continue
       return
       end
 C
```

```
Function GETTYPE
C
C
C
     Purpose:
C
        This function identifies whether a line is a character
C
        input, data input or comment.
C
C
C
      function GETTYPE(string)
      GLOBALS'
C
      character #132 string
C
     LOCALS
      integer GETTYPE, ctype(10)
      character*1 head(10)
      data head /'!','@','#','$','%','&','*','C','c',' '/
      data ctype /-1,-1,-1,-1,-1,-1,-1,-1,0/
C
     LOGIC
      GETTYPE=1
      do 100 i=1,10
        if (string(1:1) .eq. head(i)) GETTYPE=ctype(i)
100
        continue
      return
      end
File: solver.f
C=Module SOLVER
C=Purpose Solves the system of linear symmetric equations
C=Author who knows
C=Date
C=Update January 1989 by E. Pramono
C=Block Fortran
      SUBROUTINE SOLVER (BK, BR, JDIAG, NEQ, IFLAG)
      recursive SUBROUTINE SOLVER(BK, BR, JDIAG, NEQ, IFLAG)
C+----
```

THIS SUBROUTINE SOLVES THE SYSTEM OF LINEAR SYMMETRIC

- GLOBAL STIFFNESS EQUATIONS IN VECTOR FORM

IFLAG - FLAG INDICATING WHICH FUNCTION IS TO BE PERFORMED

EQUATIONS IN VECTOR FORM USING THE CROUT REDUCTION

JDIAG - LOCATION VECTOR FOR DIAGONALS IN [BK]

1 -> FORWARD REDUCTION
2 -> BACKWARD SUBSTITUTION

- GLOBAL LOAD VECTOR

NEQ - NUMBER OF EQUATIONS

C

C

C

C

C

C

C

C

C

C

PURPOSE:

METHOD.

ARGUMENTS:

BK

```
ARGUNENTS
      REAL+8 BK(1), BR(1)
      INTEGER JDIAG(1), NEQ, IFLAG
C LOCAL VARIABLES
      REAL+8 ZERO, EZERO, TOL, DAVAL, DOT, D, RDD, DD
      INTEGER LDFLAG, JR, J, JD, JH, IS, IE, K, JDT
      INTEGER JJ, ID, I, IR, IH
      JJ = 6
C
C
C
    NEW PARAMETERS
      ZERO
             = 0.000
      EZERŐ = 0.3D-14
             = 0.5D-7
      LDFLAG = 0
C
C
    FACTOR BK TO UT+D+U OR REDUCE R
      JR = 0
      DO 70 J = 1, NEQ
         JD = JDIAG(J)
         JH = JD - JR
         IS = J - JH + 2
         IF (JH - 2) 60, 30, 10
10
         IF (IFLAG .NE. 1) GOTO 50
         IE = J - 1
         K = JR + Q
         ID = JDIAG(IS-1)
C
C
    IF DIAGONAL IS ZERO COMPUTE A NORM FOR SINGULARITY TEST
C
         JDT = JDIAG(IE) + 1
         IF (BK(JD) .EQ. ZERO .AND. IFLAG .EQ. 1) THEN
            CALL DATEST (BK(JDT), JH-2, DAVAL)
         END IF
    REDUCE ALL EQUATIONS EXCEPT FIRST ROW AND DIAGONAL
         DO 20 I = IS, IE
            IR = ID
            ID = JDIAG(I)
            IH = MINO(ID-IR-1,I-IS+1)
            IF (IH .GT. 0) BK(K) = BK(K) - DOT(BK(K-IH), BK(ID-IH), IH)
            K = K + 1
20
         CONTINUE
C
C
    REDUCE FIRST ROW AND DIAGONAL
```

```
30
         IF (IFLAG .NE. 1) GOTO 50
         IR = JR + 1
         IE = JD - 1
         K = J - JD
         DD = BK(JD)
         DO 40 I = IR, IE
            ID = JDIAG(K+I)
            IF (BK(ID) .EQ. 0.0) GOTO 40
            D s BK(I)
            BK(I) = BK(I)/BK(ID)
            BK(JD) = BK(JD) - D + BK(I)
40
         CONTINUE
C
C
C
    CHECK FOR POSSIBLE ERRORS AND PRINT WARNINGS
         RDD = BK(JD)
         IF (DARS(RDD) LT. TOL+DARS(DD))
                                                  WRITE (JJ.2000) J
         IF (DD .LT. ZERO .AND. RDD .GT. ZERO)
                                                  WRITE (JJ,2001) J
         IF (DD .GT. ZERO .AND. RDD .LT. ZERO)
                                                  WRITE (JJ, 2001) J
         IF (DABS(RDD) .LT. EZERO)
                                                  WRITE (JJ,2002) J
C
C
C
    COMPLETE RANK TEST FOR A ZERO DIAGONAL TEST
         IF (DD .EQ. ZERO .AND. JH .GT. 0) THEN
            IF (DABS(RDD) .LT. TOL+DAVAL)
                                                  WRITE (JJ,2003) J
         END IF
C
C
    REDUCE RIGHT HAND SIDE
C
50
         IF (IFLAG .EQ. 2) BR(J) = BR(J) - DOT(BK(JR+1), BR(IS-1), JH-1)
60
         JR = JD
70
      CONTINUE
      IF (IFLAG .NE. 2) RETURN.
C
C
C
    DIVIDE BY DIAGONAL TERMS
      DO 80 I = 1, NEQ
         ID = JDIAG(I)
         IF (BK(ID) .NE. 0.0) BR(I) = BR(I)/BK(ID)
         IF (BR(I) .NE. ZERO) LDFLAG = 1
80
      CONTINUE
C
C
    CHECK FOR ZERO LOAD VECTOR
C
C
      IF (LDFLAG .EQ. 0) WRITE(JJ,2004)
C
C
C
    BACK SUBSTITUTE
C
      J = NEO
      JD = JDIAG(J)
90
      D = BR(J)
      J = J - 1
```

```
IF (J .LE. 0) RETURN
      JR = JDIAG(J)
      IF (JD - JR .LE. 1) GOTO 110
      IS = J - JD + JR + 2
      K = JR - IS + 1
      DO 100 I= IS, J
         BR(I) = BR(I) - BK(I+K)+D
100
      CONTINUE
      JD s JR
110
      GOTO 90
    WARNING FORMATS
2000 FORMAT(/'!! WARNING !! 1 - IN SOLVER, LOSS OF AT LEAST 7 DIGITS'
             /181, 'IN REDUCING DIAGONAL OF EQUATION;',4X,15)
     FORMAT(/'!! WARNING !! 2 - IN SOLVER, SIGN OF DIAGONAL CHANGED'
             /18X, 'WHEN REDUCING EQUATION;',15X,I5)
2002 FORMAT(/'!! WARNING !! 3 - IN SOLVER, REDUCED DIAGONAL IS ZERO'
             /18X, 'FOR EQUATION;',25X,15)
    FORMAT(/'!! WARNING !! 4 - IN SOLVER, RANK FAILURE FOR A ZERO'
             /181, 'UNREDUCED DIAGONAL IN EQUATION;',71,15)
2004 FORMAT(/'!! WARNING !! 5 - IN SOLVER, ZERO LOAD VECTOR')
      END
C=End Fortran
C=Module DATEST
C=Block Fortran
      SUBROUTINE DATEST(A,JH,DAVAL)
      recursive SUBROUTINE DATEST(A,JH,DAVAL)
C
C
        TEST FOR RANK
        INPUTS;
                A(J) - COLUMN OF UNREDUCED ELEMENTS IN ARRAY
                      - NUMBER OF ELEMENTS IN COLUMN
                DAVAL - SUN OF ABSOLUTE VALUES
C
    ARGUMENTS
      REAL+8 A(1), DAVAL
      INTEGER JH
    LOCAL ARGUNENTS
      INTEGER J
      DAVAL = 0.0D0
      DO 10 J = 1, JH &
         DAVAL = DAVAL + DABS(A(J))
10
      CONTINUE
      RETURN
      END
```

```
CsEnd Fortran
CaModule DOT
C=Block Fortran
      FUNCTION DOT(A,B,N)
      recursive FUNCTION DOT(A,B,N)
C+
C
      PURPOSE:
C
         THIS FUNCTION SUBROUTINE PERFORMS THE DOT PRODUCT OF TWO
C
         VECTORS.
C
C
     ARGUMENTS:
         A - FIRST VECTOR INVOLVED IN DOT PRODUCT
C
             - SECOND VECTOR INVOLVED IN DOT PRODUCT
C
             - NUMBER OF ELEMENTS IN EACH OF THE TWO VECTORS
      REAL+8 DOT, A(1), B(1)
      INTEGER N
C
      INTEGER I
C
      DOT = 0.0
      DO 10 I = 1, N
         DOT = DOT + A(I)*B(I)
10
      CONTINUE
      RETURN
      END
C=End Fortran
File: nophlag.f
C=Module NOPHLAG
C=Author K. Alvin
C=Date July 1990
C=Block Fortran
C
      Subroutine NOPHLAG
C
C
      Purpose:
C
        This subroutine solves for the structural displacement
C
        and velocity vectors at the half-step for the phase lag
C
        correction loop, and gets new measurement
C
C
C
C
      Arguments
C.
        delbeta - delta * bdamp
C
      subroutine NOPHLAG(zp)
      real*8 zp(1)
      include 'shared.inc'
```

```
C
      LOCAL VARIABLES
      integer i
      real *8 v(MAXDOF), delbeta
C
      LOGIC
C
      ADD APPLIED FORCES TO RHS AND PREPARE HASS MULTIPLIER
      do 10 i=1,ndof
        gs(i) = gs(i) + f(i)
        v(i) = (1. + delta*adamp)*q(i) + delta*qdot(i)
10
        continue
C
      SOLVE FOR RIGHT HAND SIDE, gs
      do 77 i = 1,ndof
        gs(i) = delsq*gs(i) + v(i)*mass(jdiag(i))
77
        continue
      if (bdamp .ne. 0.) then
        delbeta = delta*bdamp
        call PNVMAD(stif,jdiag,q,ndof,delbeta,gs,1.d0)
        endif
      SOLVE FOR DISPLACEMENT, q, USING RHS AND MATRIX S
C.
      call SOLVER(es,gs,jdiag,ndof,2)
      do 100 i=1,ndof
        v(i) = (gs(i)-q(i))/delta
100
        continue
      call ZEROVECT(zp.nsen)
      do 200 jj = 1,hdval
        i = hdrow(jj)
        j * hdcol(jj)
        zp(i) = zp(i) + hd(jj)*g*(j)
200
        continue
      do 250 jj = 1,hvval
        i = hvrow(jj)
        j = hvcol(jj)
        zp(i) = zp(i) + hv(jj)*v(i)
250
        continue
      return
      end
```

```
File: zerovect.f
```

```
C=Module ZEROVECT
C=Purpose Initialize vector of given length to zero
C=Author K. Alvin
C=Date May 1990
```

```
C
C
      Subroutine ZERGVECT
C
C
C
     subroutine ZEROVECT(v.n)
     real*8 v(1)
     integer n
     do 100 i=1.n
       \forall(i) = 0.40
100
       continue
     return
     end
File: lu.f
     SUBROUTINE LUFACT(A,N,PIVOT,DET,IER,NMAX)
  *********************
C
C
       SUBROUTINE FACTOR USES GAUSSIAN ELIMINATION WITH
C
       PARTIAL PIVOTING AND IMPLICIT SCALING TO DETERMINE
C
       THE L+U DECOMPOSION OF A SQUARE HATRIX "A" OF
C
       ORDER N. THE ALGORITHM ALSO FINDS THE DETERMINENT
C
       OF "A". UPON COMPLETION, THE ELEMENTS OF THE UPPER
C
       TRIANGULAR MATRIX "U" ARE CONTAINED IN THEIR RESPECTIVE
C
       LOCATIONS IN MATRIX "A". THE ELEMENTS OF MATRIX "L"
C
       ARE CONTAINED IN THE LOWER TRIANGULAR PORTION OF "A",
       BUT ARE SCRANBLED WITH RESPECT TO "U" BECAUSE OF ROW
C
C,
       INTERCHANGE OPERATIONS NOT PERFORMED ON THE ELEMENTS
Ç
       OF "L". THE VECTOR PIVOT (SEE BELOW) MUST BE USED TO
C
       UNSCRANBLE "L" IF IT IS TO BE USED FOR OTHER OPERATIONS.
C
C
       VARIABLES:
                    A=FULL SOUARE MATRIX (DOUBLE PRECISION)
                    N=ORDER OF MATRIX A (INTEGER)
C
C
                    PIVOT=VECTOR CONTAINING A RECORD OF
C
                          ROW INTERCHANGES. THE INTEGER
C
                          VALUE PIVOT(K) IS THE ROW WHICH
C
                          WAS INTERCHANGED WITH ROW K AT
C
                          FORWARD ELIMINATION STEP K. (INTEGER)
Ç
                   DET=DETERMINENT OF MATRIX A (DOUBLE PRECISION)
C
                   IER=ERROR FLAG. IF IER=1, THE MATRIX A WAS FOUND
C
                        TO BE SINGULAR, AND THE ROUTINE WAS EXITED. IF
C
                        IER=O, THE DECOMPOSITION WAS SUCCESSFUL.
C
      INTEGER PIVOT(1), IER, N, I, J, K, IO, NMAX
     REAL+8 A(NMAX,1),S(1000),C(1000),DET,TEMP
     DET=1.0D0
C
C
       FIND THE ROW NORMALIZING COEFFICIENTS S(I) FOR IMPLICIT SCALING.
```

EXIT ROUTINE IF ANY S(1)=0.0

```
DO 100 I=1.N
      S(I)=0.0D0
      DO 110 Je1.M
       IF (ABS(A(I,J)).GT.S(I)) S(I)=ABS(A(I,J))
 110
       CONTINUE
      IF (S(I).EQ.0) THEN
       IER#1
       DET=0.000
       RETURN
       end if
 100
     CONTINUE
C
C
      START FORWARD ELIMINATION STEP K
C
DO 120 K=1,N-1
C
C
     DETERMINE PIVOT ELEMENT A(IO,K) BY FINDING THE ROW IO
     BETWEEN K AND H CONTAINING THE MAXIMUM NORMALIZED
C
C
     VALUE IN COLUMN K. SET PIVOT(K)=10
     C(K)=0.0D0
     DO 130 I=K,N
       TEMP=ABS(A(I,K)/S(I))
       IF (TEMP.GT.C(K)) THEM
        C(K)=TEMP
        IC=I
        END IF
 130
       CONTINUE
      PIVOT(K)=IQ
C
     EXIT ROUTINE IF ALL VALUES IN COLUMN K AT OR BELOW
C
      THE MAIN DIAGONAL ARE EQUAL TO 0.0
      IF (C(K).EQ.O.O) THEN
       IER=1
       DET≃O.ODO
       RETURN
     INTERCHANGE ROWS IO AND K FOR COLUMNS K TO N. SKIP IF IO=K.
     SET DET =- DET IF ROWS ARE INTERCHANGED.
IF (IO.EQ.K) GOTO 150
      DET=-1.0D0+DET
      DO 140 J=K.N
       TEMP=A(K,J)
       A(K,J)=A(I0,J)
       A(IO.J)≈TEMP
       CONTINUE
 140
```

```
C
C
     ELIMINATE COLUMN K BELOW MAIN DIAGONAL BY MULTIPLYING
C
     ROW K FROM COLUMN K TO H BY A(I,K)/A(K,K) AND SUBTRACTING
C
     FROM ROW I. STORE THE MULTIPLIER FOR ROW I IN THE ELIMINATED
     COLUMN K. MULTIPLY THE RUNNING PRODUCT DET BY DIAGONAL ELEMENT A(K,K).
C
C
       DO 160 I=K+1.N
         A(I,K)=A(I,K)/A(K,K)
         DO 170 J=K+1,N
           A(I,J)=A(I,J)-A(I,K)+A(K,J)
  170
           CONTINUE
  160
         CONTINUE
       DET=DET+A(K.K)
  120
       CONTINUE
Ç
     CHECK LAST ROW/COLUMN FOR SINGULARITY. IF THERE IS NO ERROR,
C
     COMPLETE CALCULATION OF THE DETERMINENT, SET THE ERROR FLAG
C
C
     TO INDICATE NORMAL COMPLETION, AND EXIT.
C
IF (A(N,N).EQ.O.O) THEN
       IER=1
       DET=0.0D0
       RETURN
       END IF
     DET=DET=A(N,N)
     IER=0
     RETURN
     END
     SUBROUTINE LUSOLVE(A.N.B.PIVOT,NMAX)
C**
C
C
                SUBROUTINE SOLVE
C
     INTEGER PIVOT(1), N, I, J, K, NHAX
     REAL *8 A(NMAX,1),B(1),TEMP
     DO 100 K=1.N-1
        IF (PIVOT(K).EQ.K) GOTO 110
       TEMP=B(K)
       B(K)=B(J)
       B(J)=TEMP
       DO 120 I=K+1,N
  110
          B(I)=B(I)-A(I,K)+B(K)
  120
         CONTINUE
  100
       CONTINUE
     B(N)=B(N)/A(N,N)
     DO 130 I=N-1,1,-1
       DO 140 J=I+1,N
         B(I)=B(I)-A(I,J)+B(J)
  140
          CONTINUE
       B(I)=B(I)/A(I,I)
       CONTINUE
  130
     RETURN
     END
```

```
C=END FORTRAM
CEDECK FACTA
c=PURPOSE - Factors the A matrix as L U = A, with partial pivoting
c=AUTHOR W K BELVIE, Sept. 24, 1987
      Input
E
           amat----[n X n] matrix to be factored, destroyed on output
                  --problem size
      Output
           amat ---- contains the LU decomposition
C
      subroutine FACTA(amat,np,nrow,lp)
      real+8 amat(+),eta
      integer lp(*)
c
      do 50 i=1,np
  50
      lp(i)=i
c
      Find largest pivot.
c
c
       do 100 k=1,np-1
       amark=0.
       mmax=0
         do 200 msk,np
           if (abs(amat(lp(m)+(k-1)+nrow)) .gt. amaxk) then
             amark=abs(amat(lp(m)+(k-1)+nrow))
             MINAY STR
           endif
         continue
  200
c
           1=1p(k)
           1p(k)=1p(mmax)
           lp(mmax)=1
         do 400 i=k+1,np
           \texttt{eta=amat}(lp(i)+(k-i)+nrow)/amat(lp(k)+(k-i)+nrow)
           amat(lp(i)+(k-1)*nrow)=eta
              do 500 j=k+1,np
                 amat(lp(i)+(j-1)*nrow)=amat(lp(i)+(j-1)*nrow)-
                 eta+amat(lp(k)+(j-1)+nrow)
  500
               continue
  400
         continue
  100 continue
      return
      end
C END FORTRAM
c=DECK LUSOLV
c=PURPOSE - Solve L U x = b,
c=AUTHOR W K BELVIN, Sept. 24, 1987
```

```
C
    First solves L y = b, then U x = y
Ç
c
    Input
           amat----[n I n] matrix factored by FACTA
c
C
          np----problem size
               --pointer vector based on pivoting
C
           1p
           rhs----RHS of equation
C
C
c
     Output
           amat --- contains the LU decomposition .
¢
c
           x-----the solution vector
      subroutine LUSOLV(amat,np,nrow,1p,rhs,x)
c
      real *8 amat(*), x(*), rhs(*) .
      integer lp(*)
c
     do 50 i=1,np
     x(i)=rhs(i)
 50 continue
C
      Solve Lover System-----
c+++ Outer loop
    do 100 k=1,np
       rhs(k)=x(lp(k))
       if (rhs(k) .eq. 0.) go to 100
c**** Inner loop
       do 200 i=k+1,np
          x(lp(i))=x(lp(i))-amat(lp(i)+(k-1)*nrow)*rhs(k)
 200
        continue
100 continue
c
    Solve Upper System-----
      do 300 k=np,1,-1
       x(k)=rhs(k)/amat(lp(k)+(k-1)+nrow)
          do 400 i=1,k-1
            rhs(i)=rhs(i)-x(k)+amat(lp(i)+(k-1)+nrow)
400
          continue
 300 continue
      return
      end .
File: prepcon.f
```

```
C=Module PREPCON
C=Purpose Preprocess control analysis module for ACSIS
C=Author K. Alvin
C=Date June 1990
C=Block Fortran
Ç
       Subroutine PREPCON
```

```
C
 C
        Purpose:
           This subroutine prepares ec, the control prediction integration
 C
           matrix and eo, the observer construct matrix S (M+delta*D+delsq*K)
 C
 C
 C
 C
 C
       subroutine PREPCON
       include 'shared.inc'
. C
       LOCAL VARIABLES
       real*8 mc,kc
       integer ier
 C
       LOCIC
       call READCON
 C
     / Form Control Prediction Integration Coefficient Matrix
 C
         contype = -i : Full State Feedback
 C
 C
         contype = 0 : Luenberger Observer
         contype * +1 : Kalman Filter
       do 10 i = 1, nact + nsen
         do 20 j = 1,nact + nsen
           ec(i,j) = 0.d0
 20
           continue
 10
         continue
       if (contype) 100,200,400
 100
      ncsi = nact
       do 110 i = 1,nact
         do 120 jj = 1,bval
           j = bcol(jj)
           k = brow(jj)
           ec(i,j) = ec(i,j) + delta*f2(i,k)*b(jj)/mass(jdiag(k))
 120
           continue
 110
         continue
       goto 600
 200
       ncsi = nact + nsen
       do 210 i = 1, mact
         do 220 jj = 1,bval
           j = bcol(jj)
           k = brow(jj)
           ec(i,j) = ec(i,j) + delta = f2(i,k) = b(jj)/mass(jdiag(k))
 220
           continue
         do 240 j = nact+1,ncsi
           do 250 k = 1,ndof
              ec(i,j) = ec(i,j) + delta*f2(i,k)*l2(k,j-nact)
```

```
250
            continue
240
          continue
210
        continue
      do 260 ii = 1,hvval
        i = nact + hvrow(ii)
        do 270 jj = 1,bval
          j = bcol(jj)
          k = brow(jj)
          if (hycol(ii) .ne. k) goto 270
          ec(i,j) = ec(i,j) + delta*hv(ii)*b(jj)/mass(jdiag(k))
270
          continue
        do 290 j = nact+1,ncsi
          k = hvcol(ii)
          ec(i,j) = ec(i,j) + delta*hv(ii)*l2(k,j-nact)
290
          continue
260
        continue
      goto 600
400
      ncsi = nact + nsen
      do 470 i = 1,nact
        do 480 jj = 1,bval
          j = bcol(jj)
          k = brow(jj)
          ec(i,j) = ec(i,j) + delta*f2(i,k)*b(jj)/mass(jdiag(k))
480
          continue
        do 500 j = nact+1,ncsi
          do 510 k = 1,ndof
            ec(i,j) = ec(i,j) + delta*f2(i,k)*l2(k,j-nact)/
                       mass(jdiag(k))
510
            continue
500
          continue
470
        continue
      do 520 ii = 1.hvval
        i = nact + hvrow(ii)
        do 530 jj = 1,bval
          j = bcol(jj)
          k = brow(jj)
          if (hycol(ii) .ne. k) goto 530
          ec(i,j) = ec(i,j) + delta*hv(ii)*b(jj)/mass(jdiag(k))
530
          continue
        do 550 j = nact+1,ncsi
          k = hvcol(ii)
           ec(i,j) = ec(i,j) + delta*hv(ii)*l2(k,j-nact)/
                     mass(jdiag(k))
550
          continue
520
        continue
600
      continue
      do 1100 i = 1,ncsi
        ec(i,i) = ec(i,i) + 1.d0
1100
        continue
C
      FACTORIZE ec
      call FACTA(ec,ncsi,MAXCSI,pivot)
```

```
if (ier .eq. 1) then
        print *, 'PREPCON: Singular Matrix for Control Integration'
        endif
    Form Observer Integration Coefficient Matrix, ec
      mc = 1. + delta*adamp
      kc * delta*bdamp + delsq
      do 1200 i=1 mlen
        eo(i) = mc+mass(i) + kc+stif(i)
1200
        continue
C
      FACTORIZE ...
      call SOLVER(eo,go,jdiag,ndof,1)
C
      Initialize Observer States
      call ZEROVECT(qo, mdof)
      call ZEROVECT(qedot, ndof)
      call ZEROVECT(pe, ndof)
      return
      end
File: control.f
C=Module CONTROL
C=Author K. Alvin
C=Date May 1990
C=Block Fortran
C
      Subroutine CONTROL
C
C.
      Purpose:
C
         This subroutine carries out the numeric integration of one time
C
         step of the control system.
C
C
C
Ç
      Arguments.
C
                    estimated displacement vector at half time step
        q.p
C
                    estimated velocity vector at half time step
C
        рp
                    generalized momentum (f-D*qedotp-K*qep)
C
        z
                   measured sensor output
      subroutine CONTROL(z)
      include 'shared.inc'
      real *8 z(1)
C
      LOCAL VARIABLES
```

real #8 qep(MAXDOF),qedotp(MAXDOF),pp(MAXDOF),v(MAXDOF)

```
Ç
      LOGIC
C
      Form RHS of Control Prediction Equation Set
C
C
        contype = -i : Full State Feedback
        contype = 0 : Luenberger Observer with L1 = 0
C
C
        contype = +1 : Kalman Filter W/generalized momentum variable
      call ZEROVECT(gc,ncsi)
      if (contype) 100,200,300
100
      continue
      do 110 i = 1,ndof
        qe(i) = q(i)
        qedot(i) = qdot(i)
110
        continue
200, continue
      do 210 i = 1,ndof
        qep(i) = qe(i) + delta*qedot(i)
        qedotp(i) = qedot(i)
        pp(i) = f(i) - mass(jdiag(i)) + adamp + qedotp(i)
        v(i) = qep(i) + bdamp*qedotp(i)
210
        continue
      call PMVMAD(stif,jdiag,v,ndof,-1.d0,pp,1.d0)
      do 220 i=1,nact
        do 230 j = 1,ndof
          gc(i) = gc(i) - f1(i,j)*qep(j) - f2(i,j)*(qedot(j) +
                  delta*pp(j)/mass(jdiag(j)))
230
          continue
220
        continue
      if (ncsi .eq. nact) goto 600
      do 240 i=nact+1.ncsi
        k = i - nact
        gc(i) = z(k)
240
        continue
      do 245 ii = 1,hdval
        i = hdrow(ii) + nact
        j = hdcol(ii)
        gc(i) = gc(i) - hd(ii)*qep(j)
245
        continue
      do 250 ii = 1.hvval
        i = hvrow(ii) + nact
        j = hvcol(ii)
        gc(i) = gc(i) - hv(ii)*(qedot(j)+delta*pp(j)/mass(jdiag(j)))
250
        continue
      goto 600
300
      continue
      do 310 i = 1,ndof
```

```
qep(i) = qe(i)
        pp(i) = f(i) - mass(jdiag(i)) *adamp *qep(i)/delta
        \forall(i) = (i + bdamp/delta)*qep(i)
310
        continue
      call PMVMAD(stif,jdiag,v,ndof,-1.d0,pp,1.d0)
      do 320 i=1,nact
        do 330 j = 1,ndof
          gc(i) s gc(i) = f1(i,j)*qep(j) - f2(i,j)*(pe(j) +
                   delta*pp(j))/mass(jdiag(j))
330
          continue
320
        continue
      do 340 imnact+1,ncsi
        k = i = nact
        gc(i) = g(k)
340
        continue
      do 345 ii = 1,hdval
        i = hirow(ii) + mact
        j = hdcol(ii)
        gc(i) = gc(i) - hd(ii) + qep(j)
345
        continue
      do 350 ii = 1,hvval
        i = hvrow(ii) + nact
        j = hvcol(ii)
        gc(i) = gc(i) - hv(ii)*(pe(j) + delta*pp(j))/mass(jdiag(j))
350
        continue
      FIND r, CONTROL AND STATE CORRECTION FORCES
C
600
      call LUSQLV(ec,ncsi, MAXCSI, pivot,gc,r)
      do 610 j=1,nact
        u(j) = r(j)
610
        continue
      do 620 j=nact+1,ncsi
        gamma(j-nact) = r(j) .
620
        continue
      FIND CONTROL CONTRIBUTION TO RHS VECTOR FOR
C
      OBSERVER AND STRUCTRE
      do 710 i=1,ndof
        g*(i) = 0.40
        go(i) = 0.40
        gk(i) = 0.40
710
        continue
      do 720 jj=1,bval
        i = brow(jj)
        j = bcol(jj)
        gs(i) = gs(i) + b(jj)*u(j)
        go(i) = go(i) + b(jj)*u(j)
        gk(i) = gk(i) + b(jj)*u(j)
720
        continue
      if (contype .eq. 0) then
        do 725 i = 1,ndof
          do 730 j=1,nsen
            go(i) = go(i) + mass(jdiag(i))*12(i,j)*gamma(j)
730
            continue
```

```
725
          continue
      elseif (contype .eq. 1) then
        do 735 i = 1.ndof
          do 740 j=1,nsen
            go(i) = go(i) + (12(i,j)+mass(jdiag(i))+11(i,j)/delta)
                             *gamma(j)
            gk(i) = gk(i) + 12(i,j)*gamma(j)
740
            continue
735
          continue
          endif
      return
      end
File: secorder.f
C=Module SECORDER
C=Author K. Alvin
C=Date May 1990
C=Block Fortran
C
      Subroutine SECORDER
C
C
      Purpose:
C.
C
        Solves the second-order dynamical equation:
C
C
          Mx'' + Dx' + Kx = 1 + g
C
C.
        at time (n+1) given f(n+1/2), g(n+1/2) and x,x' at n by
C
        the midpoint implicit integration rule.
C
        Step size is 2*delta.
C
C
        D is of the form (alpha*H + beta*K), f is an applied force,
C
        and g is assumed to be other applied force from a feedback
C
        control loop. The matrix E is the factored form of the
C
        integration coefficient matrix: E=(N + delta*D + delta*2*K).
C
C
C
C
      Arguments:
C
C
                    matrix M
C
                    matrix K
        k
C
                    scalar alpha
        alpha
C
        beta
                    scalar beta
C
        ſ
                    Force vector f(n+1/2)
C
                 - Feedback force vector g(n+1/2)
        g
C
                    martix E
C
                    Variable vector x(n)
        x
Ç
                    Variable vector x'(n)
        xd
C
        delta
                    Half of integration time step
```

C

delsq

jdiag

delta-2

- Diagonal location pointer for M,K,E matrices

- Number of equations and length of q

```
- mass multiplier for RHS preparation
C
        delbeta - delta * beta
C
      subroutine SECORDER(m,k,alpha,beta,f,g,e,x,xd,
          delta, delsq, jdiag, adof, MAXDOF)
      recursive subroutine SECORDER(m,k,alpha,beta,f,g,e,x,xd,
          delta, delsq, jdiag, ndof, MAXDOF)
C
      ARGUMENTS
      real=8 m(1),k(1),alpha,beta,f(1),g(1),e(1)
      real*8 x(1),xd(1),delta,delsq
      integer jdiag(1),ndof,MAXDOF
C
      LOCAL VARIABLES
    · integer i
      real#8 v(3000),delbeta
C
      LOGIC
      ADD APPLIED FORCES TO RHS AND PREPARE MASS MULTIPLIER
      do 10 i=1,ndof
        g(i) = g(i) + f(i)
        v(i) = (1. + delta*alpha)*x(i) + delta*xd(i)
10
        continue
C
      SOLVE FOR RIGHT HAND SIDE, g.
      do 77 i=1,ndof
        g(i) = delsq*g(i) + v(i)*m(jdiag(i))
77
        continue
      if (beta .ne. 0.) then
        delbeta = delta*beta
      Activate EBE computations for internal force by using STIFFRC
C
      subroutine. Otherwise use PHVHAD (profile matrix/vector mult-add
C
        call PMVMAD(k,jdiag,x,ndof,delbeta,g,1.d0)
        call STIFFRC(x,delbeta,g)
        endif
      SOLVE FOR DISPLACEMENT, q, USING RHS AND MATRIX E
      call SOLVER(e,g,jdiag,ndof,2)
      do 100 i=1,ndof
        xd(i) = 2.*(g(i) - x(i))/delta - xd(i)
        x(i) = 2.*g(i) - x(i)
100
        continue
      return
      end
```

File: measure.f

```
C=Module MEASURE
C=Author K. Alvin
C=Date May 1990
C=Block Fortran
C
      Subroutine MEASURE
¢
C
      Purpose:
C
        This subroutine stores new measured sensor data by using the
C
        previous displacement and velocity vectors at the sensor
C
C
C
C
C
      Arguments
C
        zp - measured sensor data array
      subroutine MEASURE(zp)
      include 'shared.inc'
      real*8 zp(1)
      call ZEROVECT(zp,nsen)
      do 100 jj = 1,hdval
        i = hdrow(jj)
        j = hdcol(jj)
        zp(i) = zp(i) + hd(jj)*q(j)
100
        continue
      do 200 jj = 1,hvval
        i = hwrow(jj)
        j = hvcol(jj)
        zp(i) = zp(i) + hv(jj)*qdot(j)
200
        continue
      return
      end
File: eigens.f
```

```
include 'shared.inc'
    LOCAL VARIABLES
      parameter (NVH=100, MNHVM=NAXDOF=NVH, MXCNV=NVH=(NVH+1)/2)
      integer isl(MAXDOF), nvec, i, j, k, kk, out
      real #8 vl(NNNVN), vr(NNNVN), akk(NXCNV), amm(NXCNV)
      real*8 xx(NVM,NVM),eigv(NVM),eigold(NVM)
      real+8 toleig, toljac, omega, fhz
      toleige.0001
      out = 13
      toljac = toleig
      hvec = min0(2*neig,100)
      nwec = min0(nwec,ndof)
    SET UP ISL VECTOR
      isl(1) = 1
      do 50 j=2,ndof
        isl(j) = j - jdiag(j) + jdiag(j-1) + 1
50
        continue
    CALL EIGENSOLVER
```

call SSPACE(stif, mass, vl, vr, akk, amm, xx, eigv, eigold, isl, jdiag, neig, nvec, ndof, toleig, toljac, out)

## WRITE OUTPUT

```
write(out,*) 'EIGEN ANALYSIS RESULTS:'
      write(out,*) '
                                               RADIAL
                                                              CYCLIC,
      write(out,*) ' MODE
                               EIGENVALUE
                                              FREQUENCY
                                                             FREQUENCY
      write(out,*) ' ----
      write(out,*)
      do 100 i≈1, neig
        omega = dsqrt(eigv(i))
        fhz = omega/(2*3.141592654)
        write(out,'(i5,3(3x,g12.5))') i,eigv(i),omega,fhz
100
        continue
      write(out, *) 'EIGENVECTORS:'
      do 200 j=1,neig,5
        write(out,*)
        do 300 i=1,ndof
          k = ndof*(j-1) + i
          write(out, '(i5,5(1x,g12.5))') i,(vr(kk),kk=k,k+4*ndof,ndof)
300
          continue
200
        continue
      write(out, *) 'MASS MATRIX DIAGONAL:'
      do 400 i=1.nnp
       do 450 j=1,6
        if (id(j,i).ne.0) then
          write(out,*) i,j,id(j,i),mass(jdiag(id(j,i)))
          endif
450
        continue
```

```
400
       continue
      return
      end
C=End Fortran
File: singeig.f
      SUBROUTINE SSPACE (AK, AM, VL, VR, AKK, AMM, XX, EIGV, EIGOLD, ISL,
         IDIAG, HEIG, NVEC, NDOF, TOLEIG, TOLJAC, NW)
¢
     input :
c
             AK
                                               (profile values) (NDOF)
Ç
                    : stiffness matrix
             AM
                    : consistent mass matrix (profile values) (NDOF)
c
                    : stores in position "i" the row # of tip of
             ISL
c
                      column "i" (NDOF)
c
             IDIAG : position of diagonal terms in profile
                                                                 (NDOF)
¢
             NEIG : * of required eigenvalues
c
             NVEC
                   : # of subspace vectors
c
             NDOF
                    : * of degrees of freedom
             TOLEIG : tolerance for eigenvalues convergence
             TOLJAC : tolerance for Jacobi convergence
                    : logical unit number for output
     output:
c
c
             VL(NDOF, NVEC)
                                      : working array
                  - VL(.,1..NRMOD)
                                       : AM times rigid modes
c
                   - VL(.,NRMOD..NVEC) : subspace at the previous step
c
c
             VR(NDOF, NVEC)
                                       : eigen-vectors
C
                - VR(.,1..NRMOD)
                                       : rigid modes
c
                  - VR(.,NRMOD..NVEC) : subspace at this step (eigenvectors)
c
c
                                       : stiffness matrix in the subspace
             AKK(NVEC*(NVEC + 1)/2)
c
             AMM(NVEC+(NVEC + 1)/2)
                                       : consistent mass matrix in the subspace
C
             II(NVEC+NVEC)
                                        : subspace eigenvectors
c
c
             EIGV(NVEC)
                                       : current eigenvalues
c
                   - EIGV(1..NRMOD)
                                       : O eigen-values
¢
                   - EIGV(NRMOD..NVEC) : following eigenvalues > 0
c
c
             EIGOLD(NVEC)
                                        : same as EIGV
C
c
      IMPLICIT REAL+8 (A-H,0-Z)
      DIMENSION AK(1), AM(1), VL(NDOF, NVEC), VR(NDOF, NVEC), AKK(1),
     1 AMM(1), XX(NVEC+NVEC), EIGV(1), EIGOLD(1), ISL(1), IDIAG(1)
C
```

```
WRITE (NW, 1003) NEIG, NVEC, NDOF, TOLEIG
CALL INVECT (AK, AM, VL, VR, IDIAG, NDOF, NVEC)
CALL FACT (AK, IDIAG, ISL, NDOF, NW)
CALL NULL (AK, AM, VL, VR, IDIAG, ISL, NDOF, NRMOD)
```

```
¢
C
              NRMOD : # of rigid modes
C
      WRITE (NW, 1004) NRMOD
      MSUB=NVEC-NRMOD
C
      CALL ORTHO (VR, VL, MOOF, MRHOD, NVEC)
C
      WITEO
      MSMAI=15
      NITEAX=16
      HVEC1=HVEC-1
      DO 5 I=1, NVEC
      EIGOLD(I)=0.0
 500
      NIT=NIT+1
      WRITE (NW, 1000) HIT
C
      CALL SOLVES (AK VL(1 WENDD+1), VR(1 MENDD+1), IDIAG, ISL, NDOF, NSUB)
      CALL ORTHO (VL, VR, NDOF, NRMOD, NVEC)
C
      DO 10 J=NPAOD+1,NVEC
C
C
         CALCULATE THE UPPER PART OF AKK (SYMMETRIC)
C
         DO 10 I=NRMOD+1,J
             TR=0.0
             DO 11 K=1, NDOP
                TR=TR+VL(K,I)*VR(K,J)
  11
             IJ=IJ+1
             AKK(IJ) STR
  10
      CONTINUE
      CALL MULT (AM, VR(1, NRMOD+1), VL(1, NRMOD+1), ISL, IDIAG, NSUB, NDOF)
C
      IJ=0
      DO 20 J=NRMOD+1,NVEC
C.
         CALCULATE THE UPPER PART OF AMM (SYMMETRIC)
C.
C
         DO 20 I=NRMOD+1,J
             TR=0.0
             DO 21 K=1,NDOF
                TR=TR+VL(K,I)+VR(K,J)
  21
             IJ≈IJ+1
             AMM(IJ)=TR
  20
      CONTINUE
C
      CALL JACOBI (AKK, AMM, XX, EIGV(NRMOD+1), NSMAX, TOLJAC, NSUB, NW)
C
      ORDER EIGENVALUES & EIGENVECTORS
C
  30
     IS=0
      DO 40 I=NRMOD+1,NVEC1
          IF (EIGV(I+1).GE.EIGV(I)) GO TO 40
          IS=1
          TR=EIGV(I+1)
          EIGV(I+1)=EIGV(I)
```

```
EIGV(I)=TR
         DO 41 J=1, NSUB
            TR=XX(J+(I-NRMOD)+NSUB)
            XX(J+(I-NRMOD)=NSUB)=XX(J+(I-NRMOD-1)=NSUB)
            II(J+(I-NRMOD-1)+NSUB)=TR
  40 CONTINUE
      IF (IS.EQ.1) GO TO 30
C
C
      SUBSPACE CONVERGENCE TEST
C
      ICOHV=0
      DO 50 I=NRMOD+1,NVEC
         TR=DABS((EIGOLD(I)-EIGV(I))/EIGV(I))
         EIGOLD(I)=EIGV(I)
         EIGV(I)=TR
         IF (TR.GT.TOLEIG.AND.I.LE.NEIG) ICONV=1
  50 CONTINUE
      WRITE (NW,1001) (EIGV(I), I=1, NVEC)
      IF (ICDMY.EQ.0) GD TD 100
C
      IF (NIT.LE.NITMAX) GO TO 70
      WRITE (NW, 1002)
      GO TO 100
C
C
      UPDATE EIGEN VECTORS
C
  70 DO 80 I=1,NDOF
         DO 80 J=1,NSUB
            TR=0.0 ·
            DO 81 K=1,NSUB
               TR=TR+VR(I,K+NRMOD)+XX(K+(J-1)+NSUB)
  81
            VL(I,J+NRMOD)=TR
  80 CONTINUE
      DO 90 I=1,NDOF
         DO 90 J=NRMOD+1,NVEC
  90
         VR(I,J)=VL(I,J)
      GO TO 500
C
C
      CALCULATE FINAL EIGENVECTORS
C
 100 DO 110 I=1,NDOF
         DO 110 J=1,NSUB
            TR=0.0
            DO 111 K=1,NSUB
               TR=TR+VL(I,K+NRMOD)=XX(K+(J-1)=NSUB)
 111
            VR(I,J+WRMOD)=TR
      CONTINUE
 110
      DO 112 I=1,NVEC
 112
         EIGV(I)=EIGOLD(I)
C
      RETURN
C
 1000 FORMAT (51,12HITERATION NO,15)
 1001 FORMAT (6(2X,1PE10.3))
 1002 FORMAT (51,24HWE ACCEPT CURRENT VALUES)
 1003 FORMAT (//201,'SUBSPACE ITERATION ROUTINE'//' NB OF EIGENVALUES=',
     1 I5/' WB OF VECTOR=', I5/' WB OF DOF=', I5/' TOLERANCE=', IPE10.3/)
 1004 FORMAT (' NB OF RIGID MODES=',15//)
```

```
END
SUBROUTINE INVECT (AK, AK, VL, VR, IDIAG, NDOF, NVEC)
     IMPLICIT REAL+8 (A-H,0-Z)
     DIMENSION AK(1), AM(1), VL(1), VR(NDOF, NVEC), IDIAG(1)
C
     MD=MDOP/MVEC
C
     DO 10 I=1,NDOF
        IIsDIAG(I)
        VR(I,1) = AM(II)
        VL(I)=AH(II)/AK(II)
        DO 10 J=2,NVEC
          VR(I,J)=0.0
     CONTINUE
 10
     ll=ndop-nd
C
     DO 20 J=2, IVEC
        TR=0.0
C
        DO 30 I=1,LL
          IF (VL(I).LT.TR) GO TO 30
          TR=VL(I)
          ŢĴ≊Ţ
        CONTINUE
 30
C
        DO 40 I=LL NDOF
          IF (VL(I).LE.TR) GO TO 40
          TR=VL(I)
          IJzľ
        CONTINUE
 40
C
        VL(IJ)=0.0
        LL=LL-ND
        VR(IJ,J)=1.0
C
     CONTINUE
 20
C
     RETURN
SUBROUTINE HULT (AM, VR, VL, ISL, IDIAG, NVEC, NDOF)
     IMPLICIT REAL+8 (A-H,0-2)
     DIMENSION AM(1), VR(MDOF, NVEC), VL(MDOF, NVEC), ISL(1), IDIAG(1)
     DO 500 IV=1,NVEC
        DO 100 I=1,NDOF
           TR=0.0
           IJ=IDIAG(I)
           IK=ABS(ISL(I))
           KK⇒I
           DO 110 K=IK,I
             TR=TR+AM(IJ) +VL(KK, IV)
             IJ=IJ-1
             KK=KK-1
110
           CONTINUE
C
           IF (I.EQ.NDOF) GO TO 99
```

```
IK=I+1
            DO 120 K=IK, NDOP
               IF (I.LT.ABS(ISL(K))) GO TO 120
               IJ=IDIAG(K)-K+I
               TR=TR+AM(IJ)*VL(K,IV)
 120
            CONTINUE
 99
            VR(I,IV)=TR
 100
         CONTINUE
 500
      CONTINUE
      RETURN
      END
SUBROUTINE JACOBI (AK, AM, XX, EIGV, NSMAX, TOL, N, NV)
      IMPLICIT REAL+8 (A-H, 0-Z)
      DIMENSION AK(1), AM(1), XX(N,N), EIGV(1)
C
C
     INITIALIZE
.2
     ZERO=0.0
      TW0=2.0
      DO 10 I=1,N
         II=I*(I-1)/2+I
         IF (AK(II).LE.ZERO.OR.AM(II).LE.ZERO) GO TO 900
         EIGV(I)=AK(II)/AH(II)
         DO 20 J=1,N
            XX(I,J)=ZERO
  20
         CONTINUE
         XX(I,I)=1.0
  10
      CONTINUE
C
C
      SET COUNTER
C
      NSWEEP=0
      NR=N-1
 500
      NSWEEP=NSWEEP+1
C
C
      CHECK IF ZEROOING IS REQUIRED
C
      EPS=0.01**NSWEEP
      EPS=EPS*EPS
      DO 150 J=1,NR
         IIK=J+1
         DO 150 K=IIK.N
            JJ=J+(J-1)/2+J
            KK=K+(K-1)/2+K
            JK=K*(K-1)/2+J
            EPSAK=(AK(JK)+AK(JK))/(AK(JJ)+AK(KK))
            EPSAM=(AM(JK)+AM(JK))/(AM(JJ)+AM(KK))
            IF (EPSAK.LT.EPS.AND.EPSAM.LT.EPS) GO TO 150
C
C
            CALCULATE ROTATION ELEMENTS
            AKK=AK(KK)*AM(JK)-AM(KK)*AK(JK)
            AJJ=AK(JJ)+AM(JK)-AM(JJ)+AK(JK)
            AB=(AK(JJ)+AM(KK)-AK(KK)+AM(JJ))/TWO
            CHECK=AB+AB+AKK+AJJ
            IF (CHECK.LT.ZERO) GO TO 900
            SQCH=DSQRT(CHECK)
```

```
D1=AB+SQCH
             D2=AB-SQCH
             DEN=D1
             IF (DABS(D2).GT.DABS(D1)) DEN=D2
             IF (DEM.ME.ZERO) GO TO 45
             CASZEELO
             CGs-AK(JK)/AK(KK)
             GO TO 50
  45
             CASAKK/DEN
             CGs-AJJ/DEN
C
C
             PERFORM GENERALIZED ROTATION
C
  50
             JP1=J+1
             JM1=J-1
             KP1=K+1
             KM1=K-1
             IF (JM1.LT.1) GO TO 70
            DO 60 I=1.JH1
                IJ=J#JM1/2+I
                IK=K*KM1/2+I
                AKJ=AK(IJ)
                AKK=AK(IK)
                AMJ=AM(IJ)
                AMK=AM(IK)
                AK(IJ)=AKJ+CG+AKK
                AN(IJ)=AMJ+CG+AMK
                AK(IK)=AKK+CA+AKJ
                AM(IK)=AMK+CA+AMJ
  60
            CONTINUE
  70
             IF (KP1.GT.N) GO TO 90
            DO 80 I=KP1,N
                JI*I*(I-1)/2+J
                KI=I*(I-1)/2+K
                AKJ=AK(JI)
                AMJ=AM(JI)
                AKK=AK(KI)
                AMK=AM(KI)
                AK(JI)=AKJ+CG+AKK
                AM(JI)=AMJ+CG+AMK
                AK(KI)=AKK+CA+AKJ
                AM(KI)=AMK+CA+AMJ
  80
             CONTINUE
  90
             IF (JP1.GT.KM1) GO TO 110
            DO 100 I=JP1,KM1
                JI=I+(I-1)/2+J ·
                IX=K+(K-1)/2+I
                AKJ=AK(JI)
                AMJ=AM(JI)
                AKK=AK(IK)
                AMK=AM(IK)
                AK(JI)=AKJ+CG+AKK
                AM(JI)=AMJ+CG+AMK
                AK(IK)=AKK+CA+AKJ
                AM(IK)=AMK+CA+AMJ
 100
             CONTINUE
             AKK=AK(KK)
 110
             AMK=AM(KK)
```

AKJ=AK(JJ)

```
AMJ=AM(JJ)
            AK(KK)=AKK+TWO+CA+AK(JK)+CA+CA+AKJ
            AN(KK)=ANK+TWO+CA+AN(JK)+CA+CA+ANJ
            AK(JJ)=AKJ+TWD+CG+AK(JK)+CG+CG+AKK
            AM(JJ)=AMJ+TWO+CG+AM(JK)+CG+CG+AMK
            AK(JK)=ZERO
            AM(JK)=ZERO
C
            UPDATE EIGENVECTOR FOR THIS ROTATION
C
            DO 120 I=1,N
               XXJ=XX(I,J)
               XXK=XX(I,K)
               XX(I,J)=XXJ+CG+XXK
               IX(I,K)=IXK+CA+XXJ
 120
            CONTINUE
 150
      CONTINUE
C
      IIPDATE EIGENVALUES & CHECK CONVERGENCE
C
      NT=N+(N+1)/2
      ICONV=0
      DO 160 I=1,N
         II=I*(I-1)/2+I
         IF (AK(II).LE.ZERO.OR.AM(II).LE.ZERO) GO TO 900
         TR=AK(II)/AM(II)
         DEN=(TR-EIGV(I))/TR
         EIGV(I)=TR
         IF (DABS(DEN).GT.TOL) ICONV=1
 160
     CONTINUE
      IF (ICONV.EQ.1) GO TO 499
C
C:
      CHECK OFF DIAGONAL TERMS
      EPS=TOL+TOL
      DO 170 J=1,NR
         IIK=J+1
         DO 170 K=IIK,N
            JJ=J*(J-1)/2+J
            KK=K+(K-1)/2+K
            JK=K+(K-1)/2+J
            EPSAK=(AK(JK)*AK(JK))/(AK(JJ)*AK(KK))
            EPSAM=(AM(JK)+AM(JK))/(AM(JJ)+AM(KK))
            IF (EPSAK.LT.EPS.AND.EPSAM.LT.EPS) GO TO 170
            GO TO 499
 170
      CONTINUE
C.
C
      SCALE EIGENVECTORS
C
 179
      DO 180 I=1,N
         II=I+(I-1)/2+I
         AKK=DSQRT(AM(II))
         DO 180 J=1,N
            XX(J,I)=XX(J,I)/AKK
 180
      CONTINUE
C
      RETURN
     IF (NSWEEP.LE.NSHAX) GO TO 500
 499
```

V.

```
WRITE (NW, 1000)
      GO TO 179
 900 WRITE (NV.1001)
      STOP
 1000 FORMAT (51,34HNO CONVERGENCE AT MSNAX ITERATIONS)
 1001 FORMAT (5X.46HERROR IN JACOBI : MATRIX NOT POSITIVE DEFINITE)
SUBROUTINE SOLVES (AK, VL, VR, IDIAG, ISL, NDOF, NVEC)
C
      PURPOSE : SOLVES THE SINGULAR PROBLEM : AK x VL = VR
C
                THE SINGULAR COLUMNS INTO AK ARE INDEXED BY
                THE NEGATIVE VALUES OF ISL, THE CORRESPONDING
C
C
                TERMS OF THE SOLUTION ARE PUT TO 0
¢
C
      IMPLICIT REAL+8 (A-H.O-Z)
     DIMENSION AK(1), VL(NDOF, NVEC), VR(NDOF, NVEC), IDIAG(1), ISL(1)
C
      DO 500 IV=1.NVEC
        DO 50 I=1,NDOF
  50
            VL(I,IV)=VR(I,IV)
C
C
         BACKSUBSTITUTE
         DO 100 IC=2,NDOF
            TR=0.0
            IC1=IC-1
            IN1=IDIAG(IC)-IC
            IK=ISL(IC)
            IF (IK.LE.O) THEN
               VL(IC,IV)=0.
               GOTO 100
            ENDIF
            IF (IK.GT.IC1) GO TO 100
            DO 120 K=IK, IC1
               TR=TR+AK(IN1+K)+VL(K,IV)
 120
            CONTINUE
            VL(IC, IV)=VL(IC, IV)-TR
 100
         CONTINUE
C
         SOLVE DU=U
C
C
         DO 150 IC=1,NDOF
            VL(IC, IV)=VL(IC, IV)/AK(IDIAG(IC))
         CONTINUE
 150
C
         BAKSUBSTITUTE
C
C
         IIC=NDOP
         DO 200 IC=2,NDOF
            TR=VL(IIC, IV)
            IC1=IIC-1
            IK=ISL(IIC)
            IN1=IDIAG(IIC)-IIC
```

```
IF ((IK.GT.IC1).OR.(IK.LE.O)) GO TO 221
           DO 220 K=IK,IC1
              VL(K,IV)=VL(K,IV)-AK(IN1+K)+TR
 220
           CONTINUE
 221
           IIC=IIC-1
 200
        CONTINUE
 500
     CONTINUE
     RETURN
     END
SUBROUTINE FACT (AK, IDIAG, ISL, NDOF, NW)
C
C
     PURPOSE : LDLT DECOMPOSITION OF THE POSITIVE SENI-DEFINITE
               MATRIX AK, THE SINGULAR COLUMNS OF AK ARE INDEXED
C
C
               BY A NEGATIVE VALUE OF IDIAG>
C
C
     IMPLICIT REAL+8 (A-H.O-Z)
     DIMENSION AK(1), IDIAG(1), ISL(1)
C.
C
     DETERMINE MIN & MAX
C
     TR=DABS(AK(1))
     AMIN=TR
      AMAX=TR
     DO 10 IL=1,NDOF
        TR=DABS(AK(IDIAG(IL)))
         IF (TR.LT.AMIN) AMIN=TR
         IF (TR.GT.AMAX) AMAX=TR
  10 CONTINUE
      ZERO=(AMAX+AMIN)+1.0D-10
C
C
     LOOP OVER COLUMN
C
      DO 100 IC=1.NDOF
         MIC=ISL(IC)
         IC1=IC-1
         MIC1=MIC+1
         IN2=IDIAG(IC)-IC
         IF ((MIC.LT.1).OR.(MIC.GT.IC)) GO TO 901
C
C.
         CALCULATE GS
C .
         IF (MIC1.GT.IC1) GO TO 150
         DO 120 IL=MIC1,IC1
            IF (IDIAG(IL).LT.0) THEN
              AK(IN2+IL)=0
              GOTO 120
            ENDIF
           MIL=ISL(IL)
            IL1=IL-1
            HIM=MAIO(MIL, MIC)
           IN1=IDIAG(IL)-IL
            TR=0.0
            IF (MIM.GT.IL1) GO TO 120
           DO 130 K=MIM, IL1
               TR=TR+AK(IN1+K)+AK(IN2+K)
 130
            CONTINUE
```

```
IN=IN2+IL
           AK(IN)=AK(IN)-TR
 120
        CONTINUE
C
C
        CALCULATE LAD
¢
 150
        TR=0.0
        IF (MIC.GT.IC1) GO TO 201
        DO 200 ILBEIC, IC1
           IF (IDIAG(IL).LT.0) GOTO 200
           AG=AK(IM2+IL)
           AL=AG/AK(IDIAG(IL))
           AK(IN2+IL)=AL
           TR=TR+AL+AG
 200
        CONTINUE
 201
        INSIDIAG(IC)
         AK(IM)=AK(IN)-TR
        IF (AK(IN).LT.ZERO) IDIAG(IC)=-IDIAG(IC)
 100
     CONTINUE
     RETURN
901 WRITE (NW, 1001)
     STOP
 1001 FORMAT (51,29H ** * STOP ERROR IN IDIAG VECTOR)
 1010 FORMAT (SX,'CONDITIONING OF THE STIFFNESS MATRIX'/2X,
    1 'MIN DIAG TERM=', 1PE10.3,' MAX DIAG TERM=', E10.3)
SUBROUTINE NULL (AK, AH, VL, VR, IDIAG, ISL, NDOF, NRMOD)
C
C
     PURPOSE : CALCULATE THE NULL SPACE OF AK AND PUT AN
C
               ORTHONORMALISED BASE OF THIS SPACE INTO THE
C
               NRMOD FIRST VECTORS OF VR.
C
               VL = AM x VR AFTER EXECUTION
C
¢
     IMPLICIT REAL+8 (A-H,0-Z)
     DIMENSION AK(1), AM(1), IDIAG(1), ISL(1), VL(NDOF, *), VR(NDOF, *)
C
C
     STORE THE SINGULAR COLUMNS INTO THE BEGINNING OF VR
C
C
     THE SINGULAR EQUATION ARE NOW INDEXED BY NEGATIVE VALUES
C
     INTO ISL INSTEAD OF IDIAG
     NRMOD=0
     DO 1 IC=1,NDOF
         IF (IDIAG(IC).GT.0) GOTO 1
         IDIAG(IC)=-IDIAG(IC)
        NRMOD=NRMOD+1
         MIC=ISL(IC)
         IN=IDIAG(IC)-IC
        DO 2 K=1, MIC-1
            VR(K,NRMOD)=0.
   2
         DO 3 K=MIC,IC-1
            VR(K,NRMOD)=AK(IN+K)
            AK(IN+K)=0.
         CONTINUE
   3
```

```
ISL(IC)=-ISL(IC)
         VR(IC, MRMOD)=-1.
         AK(IDIAG(IC))=1.
         DO 4 K=IC+1,NDOF
         VR(K, NRMOD)=0.
      CONTINUE
C
      BAKSUBSTITUTE
C.
      DO 200 N=1,NRMOD
         IIC=NDOF
         DO 200 IC=2.NDOF
            TR=VR(IIC, N)
            IC1=IIC-1
            IK=ISL(IIC)
            IN1=IDIAG(IIC)-IIC
            IF ((IK.GT.IC1).OR.(IK.LE.0)) GO TO 221
            DO 220 K=IK, IC1
               VR(X,H)=VR(X,H)-1K(IH1+K)«TR
 220
            CONTINUE
 221
            IIC=IIC-1
 200
      CONTINUE
      ORTHOGONALISATION.
C
C
      DO 10 N=1,NRMOD
         DO 20 K=1.N-1
            TR=0.
            DO 30 I=1,NDOF
  30
               TR=TR+VL(I,K)+VR(I,N)
            DO 40 I=1.NDOF
  40
              VR(I,N)=VR(I,N)-TR+VR(I,K)
  20
         CONTINUE
         CALL MULT(AM, VL(1,M), VR(1,M), ISL, IDÍAG, 1, NDOF)
         TR=0.
         DO 50 I=1,NDOF
  50
            TR=TR+VR(I,N)+VL(I,N)
         TR=1/SQRT(TR)
         DO 60 I=1,NDOF
            VR(I,N)=VR(I,N)+TR
            VL(I,N)=VL(I,N)+TR
  60
         CONTINUE
  10 CONTINUE
      RETURN
      END
SUBROUTINE ORTHO(VL, VR, NDOF, NRMOD, NVEC)
C
C
      PURPOSE : ORTHOGONALISE THE HSUB LAST COLUMNS OF VL (LAST
C
                EVALUATED SOLUTION) WITH RESPECT TO THE NULL SPACE
C
                OF A, FOR THE AM SCALAR PRODUCT
¢
C
      IMPLICIT REAL+8 (A-H, 0-Z)
      INTEGER NDOF, NRMOD, NVEC
      DIMENSION VL(NDOF, NVEC), VR(NDOF, NVEC)
      NSUB=NVEC-NRMOD
```

```
DO 1 J=1,NSUB
DO 2 I=1,NRMOD
S=0.
DO 3 K=1,NDOF

S=S+VL(K,I)*VL(K,NRMOD+J)
DO 4 L=1,NDOF

VL(L,NRMOD+J)=VL(L,NRMOD+J)-S*VR(L,I)

CONTINUE

RETURN
END
```

```
File: animout.f
```

```
C=Module ANIMOUT
C=Author K. Alvin
C=Date June 1990
CaBlock Fortran
C
      subroutine ANIMOUT
C
Ċ
      Purpose:
C
        This subroutine produces an output file to be used to
C
        visualize the simulation using MESH.
C
C
      subroutine ANIMOUT(q,id,nnp,time,out)
      real*8 q(1),time,v(3)
      integer out, id(6,!), nnp,i,k
      write(out, '(g15.5)') time
      do 100 i=1,nnp
        do 200 k=1,3
          if (id(k,i) .ne. 0) then
            v(k) = q(id(k,i))
          else
            v(k) = 0.
            endif
200
          continue
        write(out,1000) (v(k),k=1,3)
100
        continue
1000 format(3g15.5)
      return
      end
```

File: stiffrc.f

C subroutine STIFFRC(v,fact,kq)

```
recursive subroutine STIFFRC(v,fact,kq)
      real *8 v(1), fact, kq(1)
      include 'shared.inc'
   ASSEMBLE EACH ELEMENT MASS AND STIFFNESS
      do 100 ii=1,ndomain
CVD$ CHCALL
       do 110 jj=1,neld(ii)
        n = elnum(jj,ii)
        call ELEFRC(v,fact,kq,n)
110
        continue
100
       continue
      return
      end
C
      subroutine ELEFRC(v,fact,kq,n)
      recursive subroutine ELEFRC(v,fact,kq,n)
      real = 8 v(1), fact, kq(1)
      integer n
      include 'shared.inc'
C
      LOCAL VARIABLES
      parameter(MAISEQ=24)
      real = 8 sk(MAXSEQ, MAXSEQ)
      integer lm(MAISEQ),nseq
      do 20 k=1,4
        j=ix(k,n)
        if ((etype(n).eq.1).and.(k.gt.2)) j = 0
        do 30 i=1,6
          kk=6*(k-1) + i
          if (j .ne. 0) then
            lm(kk) = id(i,j)
          -150
            lm(kk) = 0
            endif
30
          continue
20
        continue
      nseq=12
      call LOADSK(sk,n,nseq)
      call ESTIFVM(sk,lm,nseq,v,kq,fact)
      return
      bze
```

Š . . . . . . . . . . . .

```
subroutine LOADSK(sk,n,nseq)
      recursive subroutine LOADSK(sk,n,nseq)
      include 'shared.inc'
      real *8 sk(nseq,1)
      integer n,nseq
      k=0
      do 10 j=1,nseq
        de 20 i=1,j
          kek+i
          sk(i,j)=estifm(k,n)
          sk(j,i)=sk(i,j)
20
          continue
10
        continue
      return
      end
File: estifvm.f
      subroutine ESTIFVM(sk,lm,nseq,v,kq,fact)
      recursive subroutine ESTIFVM(sk,lm,nseq,v,kq,fact)
    ARGUNENTS
      real*8 sk(nseq,1),v(1),kq(1),fact
      integer lm(1),nseq
      do 20 j = 1, nseq
         k = lm(j)
         if (k .eq. 0) goto 20
         do 10 i = 1, nseq
            m = lm(i)
            if (m .eq. 0) goto 10
kq(m) = kq(m) + sk(i,j)*v(k)*fact
10
         continue
20
      continue
      return
      end
C=End Fortran
File: renum.f
C=DECK RENUM
C=PURPOSE- RENUMBERS THE GRID POINTS TO MINIMIZE PROFILE STORAGE
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subroutine REMUM

include 'shared.inc'

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C
      Initialize vector
      maxtry=2+nnp/3 +1
      nterms=nnp*maxtry
      do 22 j=1,nterms
 22
       iadjcy(j)=0
      do 10 i=1,npp
 10
       icount(i)=0
****************
      do 1 i=1,nel
        nodea=ix(1,i)
        nodeb=ix(2,i)
           if ((nodea .eq. 0).or.(nodeb .eq. 0)) go to 1
        icount(nodea)=icount(nodea)+1
        icount(nodeb)=icount(nodeb)+1
        iswicount(nodes)
        ib=icount(nodeb)
        if(ia.gt.maxtry .or. ib.gt.maxtry) go to 345
        locate=(nodea-1) *maxtry+ia
        :adjcy(locate)=nodeb
        locate=(nodeb-1)=maxtry+ib
        iadjcy(locate)=nodea
       continue
**********
       ii=0
       do 37 i=1,nterms
         if ( iadjcy(i) .eq. 0 ) go to 37
         ii=ii+1
         iadjcy(ii)=iadjcy(i)
 37
        continue
       last=0
       do 2 i=1,nnp
             last=last+icount(i)
  2
           continue
       jj=icount(1)
       icount(1)=1
       do 3 i=2,nnp+1
         kk=icount(i)
         icount(i)=icount(i-1)+jj
         jj=kk
        continue
 3
       go to 556
 345
       write(6,555)
       format(2x,'error in dimension for MAXTRY !! ')
 555
 556
       continue
***************
       call GENRCM(nnp,icount,iadjcy,perm,mask,xls)
       end
subroutine genrom(nequs, xadj, adjncy, perm, mask, xls)
c.....reference: computer solution of large sparse positive definite
                  systems, alan george & joseph w-h liu
c.....
                  (prentive-hall, inc., englewood cliffs, NJ 07632)
       integer adjncy(1),mask(1),perm(1),xls(1)
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```
integer xadj(1),ccsize,i,neqns,nlvl,num,root
      do 100 i=1,neqns
         mask(i)=1
 100
       continue
      num=1
      do 200 i=1, nequs
        if( mask(i).eq.0 ) go to 200
        rootsi
         call inroot(root, xadj, adjncy, mask, nlvl, xls, perm(num) )
      call rcm(root, xadj, adjncy, mask, perm(num), ccsize, xls)
        numsnum+ccsize
        if(num.gt.nequs) go to 987
200
       continue
c.....perm(new node)=old node
c..... now, mask(old node)= new node
987
      continue
      do 11 newsi, nequs
        iold=perm(new)
        mask(iold)=new
        write(6,*) 'iold, mask(iold) = ',iold, mask(iold)
11
      · continue
      return
      end
subroutine fnroot(root, xadj, adjncy, mask, nlvl, xls, ls)
      integer adjncy(1),ls(1),mask(1),xls(1)
      integer xadj(1),ccsize,j,jstrt,k,kstop,kstrt,
              mindeg, nabor, ndeg, nlvl, node, nunlvl, root
      call rootls(root, xadj, adjncy, mask, nlvl, xls, ls)
      ccsize=xls(nlvl+1)~1
      if(nlvl.eq.1 .or. nlvl.eq.ccsize) return
100
      jstrt=xls(nlvl)
      mindeg=ccsize
      root=ls(jstrt)
       if(ccsize.eq.jstrt) go to 400
       do 300 jajstrt,ccsize
         node=ls(j)
        ndeg=0
        kstrt=radj(node)
        kstop=xadj(node+1)-1
         do 200 k=kstrt,kstop
          nabor=adjncy(k)
           if( mask(nabor) .gt. 0) ndeg=ndeg+1
 200
          continue
         if(ndeg.ge.mindeg) go to 300
         rootsnode
        mindeg=ndeg
 300
        continue
 400
       call rootls(root, xadj, adjncy, mask, nunlvl, xls, ls)
       if(numlvl.le.mlvl) return
       nlvl=nunlvl
       if(nlyl.lt.ccsize) go to 100
      return
       end
subroutine rcm(root, xadj, adjncy, mask, perm, ccsize, deg)
       integer adjncy(1),deg(1),mask(1),perm(1)
       integer radj(1),ccsize,fnbr,i,j,jstop,jstrt,k,l,lbegin,
               lnbr,lperm,lvlend,nbr,node,root
```

```
call degree(root, xadj, adjncy, mask, deg, ccsize, perm)
      mask(root)=0
      if(ccsize.le.1) return
      lvlend=0
      labr=1
100
      lbegin=lwlend+1
      lvlend=lnbr
      do 600 i=lbegin,lvlend
        node=perm(i)
         jstrt=xadj(node)
         jstop=xadj(node+1)-1
        fabr=labr+1
         do 200 j=jstrt,jstop
          nbreadjncy(j)
           if(mask(nbr).eq.0) go to 200
           lnbr=lnbr+1
          mask(nbr)=0
          perm(lnbr)=nbr
200
          eggitago
         if(fnbr.ge.lnbr) go to 600
        kafabr
300
         lsk
         k=k+1
         nbr=perm(k)
         if(1.lt.fnbr) go to 500
400
         lperm=perm(1)
        if( deg(lperm).le.deg(nbr) ) go to 500
        perm(1+1)=lperm
         1=1-1
         go to 400
500
        perm(l+1)=nbr
         if(k.lt.lnbr) go to 300
600
        continue
       if(lnbr.gt.lvlend) go to 100
      k=ccsize/2
      l=ccsize
      do 700 i=1.k
         lperm=perm(1)
         perm(1)=perm(i)
         perm(i)=lperm
         1=1-1
700
       continue
      return
       end
subroutine rootls(root, xadj, adjncy, mask, nlvl, xls, ls)
       integer adjncy(1),ls(1),mask(1),xls(1)
       integer xadj(1),i,j,jstop,jstrt,lbegin,ccsize,lvlend,
               lvsize, nbr, nlvl, node, root
       mask(root)=0
       ls(1)=root
      nlvl=0
       lvlend=0
       ccsize=1
200
       lbegin=lvlend+1
       lvlend=ccsize
       nlvl=nlvl+1
       xls(nlv1)=lbegin
       do 400 i=lbegin,lvlend
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nodesls(i)
         jstrt=radj(node)
         jstop=radj(node+1)-1
         if(jstop.lt.jstrt) go to 400
         do 300 j=jstrt,jstop
           abreadjacy(j)
           if( mask(nbr).eq.0) go to 300
           ccsizesccsize+1
           ls(ccsize)*nbr
           mask(nbr)=0
300
          continue
400
        continue
       lvsize=ccsize-lvlend
       if(lvsize.gt.0) go to 200
       xls(nlvl+1)=lvlend+1
       do 500 i≈1,ccsize
         nodesls(i)
         mask(node)=1
500
        continue
       return
       end
cXXXXXXXXXXXXXXXXXXXXXXXXX
       subroutine degree(root, xadj, adjncy, mask, deg, ccsize, ls)
       integer adjncy(1),deg(1),ls(1),mask(1)
       integer radj(1),ccsize,i,ideg,j,jstop,jstrt,
               lbegin, lvlend, lvsize, nbr, node, root
       ls(1)=root
       xadj(root)=-xadj(root)
       lvlend=0
       ccsize=1
100
       lbegin=lvlend+1
       lvlend=ccsize
       do 400 i=lbegin,lvlend
         node=ls(i)
         jstrt=-xadj(node)
         jstop=iabs( xadj(node+1) ) -1
         ideg=0
         if(jstop.lt.jstrt) go to 300
           do 200 j=jstrt,jstop
           nbr=adjncy(j)
           if( mask(nbr).eq.0 ) go to 200
           ideg=ideg+1
           if(xadj(nbr).lt.0) go to 200
           xadj(nbr)=-xadj(nbr)
           ccsize=ccsize+1
           ls(ccsize)=nbr
 200
          continue
 300
         deg(node)=ideg
 400
        continue
       lvsize=ccsize-lvlend
       if(lvsize.gt.0) go to 100
       do 500 i=1,ccsize
         node=ls(i)
         xadj(node)=-xadj(node)
 500
        continue
       return
       end
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File: kfilter.f

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```
subroutine KFILTER
      recursive subroutine KFILTER
      include 'shared.inc'
      do 10 i = 1,ndof
        go(i) = delsq*(f(i)+go(i))+delta*pe(i)+mass(jdiag(i))*qe(i)
        gk(i) = delta*(f(i)+gk(i))+pe(i)
10
      call SOLVER(eo,go,jdiag,ndof,2)
C
      Activate EBE computations for internal force by using STIFFRC
C
      subroutine. Otherwise use PMVMAD (profile matrix/vector mult-add
C
     call PHVMAD(stif, jdiag, go, adof, -delta, gk, 1.d0)
      call STIFFRC(go,-delta,gk)
      do 100 i = 1,ndof
        qe(i) = 2.*go(i) - qe(i)
        pe(i) = 2.*gk(i) - pe(i)
100
        continue
      return
      end
```